

# MICRO-428: Metrology

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**EPFL**

# MICRO-428: Metrology

Week Eleven: Electrical Metrology

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# Reference Books

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- 📖 *E. Charbon, "Image Sensors – ET 4390 Course Slides", Delft 2016*
- 📖 *S. Cova, "Sensors Signals and Noise – Course Slides", Politecnico di Milano 2016*  
-> link: <http://home.deib.polimi.it/cova/elet/lezioni/lezioni.htm>
- 📖 *B. Staszewski, "Practical PLL Design for Frequency Synthesis and Clocking", EPFL MEAD Course Slides, Lausanne 2016*
- 📖 *I.G. Hughes, T.P.A. Hase, Measurements and Their Uncertainties, 1<sup>st</sup> ed., 2010*
- 📖 *J.K. Blitzstein, J. Hwang, Introduction to Probability, 1<sup>st</sup> ed., 2015*

# Week 10 Summary

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10.1 **Charge, Current, Voltage:** properties (microscopic), definitions,  $I = dQ/dt$ ,  $I = V/R$  (Ohm's Law),  $P = IV = I^2R = V^2/R$  (Ohmic (Joule's) heating)

10.2 **Noise Background:**

Recap: **Noise as a Random Process (RP, §3.1).**

Stationary and **Wide-sense stationary (WSS) noise:** constant mean +  $K_{XX}(t, t + \tau) = K_{XX}(\tau)$

**Noise Power** (for WSS noise):  $K_{nn}(0) = E\{n^2(t)\} = \overline{n^2(t)}$  ( $= \sigma_n^2$  assuming 0 mean:  $\mu_n = 0$ )

Concept of Noise Spectrum and **PSD (power spectral density)**, one-sided or two-sided:

$$S_n(t_1, \omega) = \Im\{K_{nn}(t_1, \tau)\}$$

**White Noise** (spectrally flat  $\rightarrow$  constant PSD, autocorrelation = Dirac delta)

## 10.3 Noise sources:

- **Thermal noise**, e.g. in resistors. Is an example of **white noise**. Bilateral PSD:  $2kTR$ .
- **kTC noise** (thermal noise on capacitors), e.g. when opening a real switch:  $\overline{V_0^2} = \frac{kT}{C}$
- **Shot (or Poisson noise)**, e.g. current flow through a potential barrier, or in photon-counting devices.  
Bilateral PSD:  $S = qI$ , WSS white noise.

NB: thermal and shot noise are irreducible. Excess noise examples:

- **1/f** or **flicker noise**, approximatively  $1/f$  power spectrum.
- **RTS** (Random Telegraph Signal) noise.
- Other...

# Outline

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10.1 Charges, Currents, and Voltages

10.2 Noise Background

10.3 Noise Sources

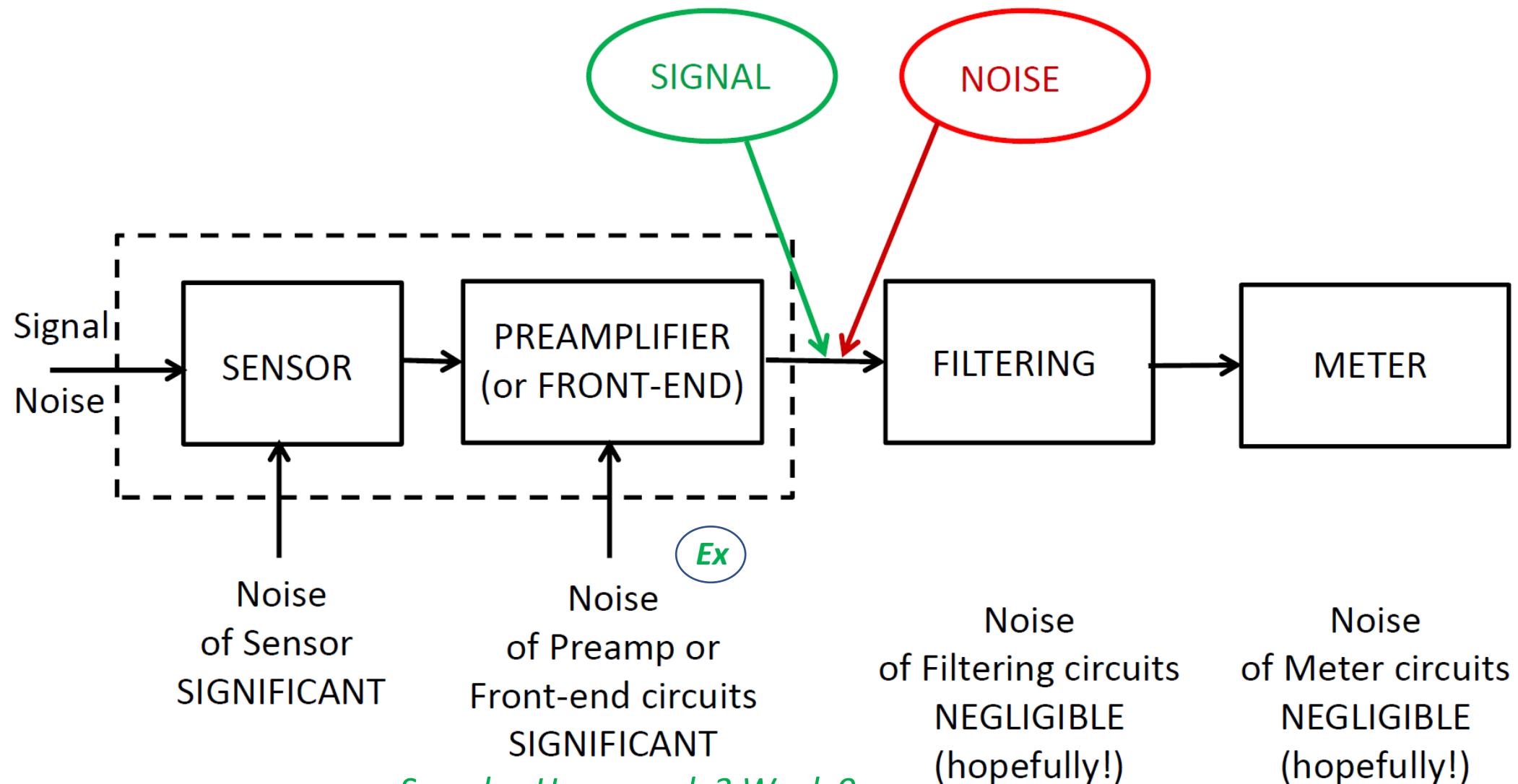
11.1 **Noise Reduction, Averaging Techniques**

11.2 Electric Signals, Analog-to-Digital Conversion

11.3 Timing – Time-to-Digital Conversion

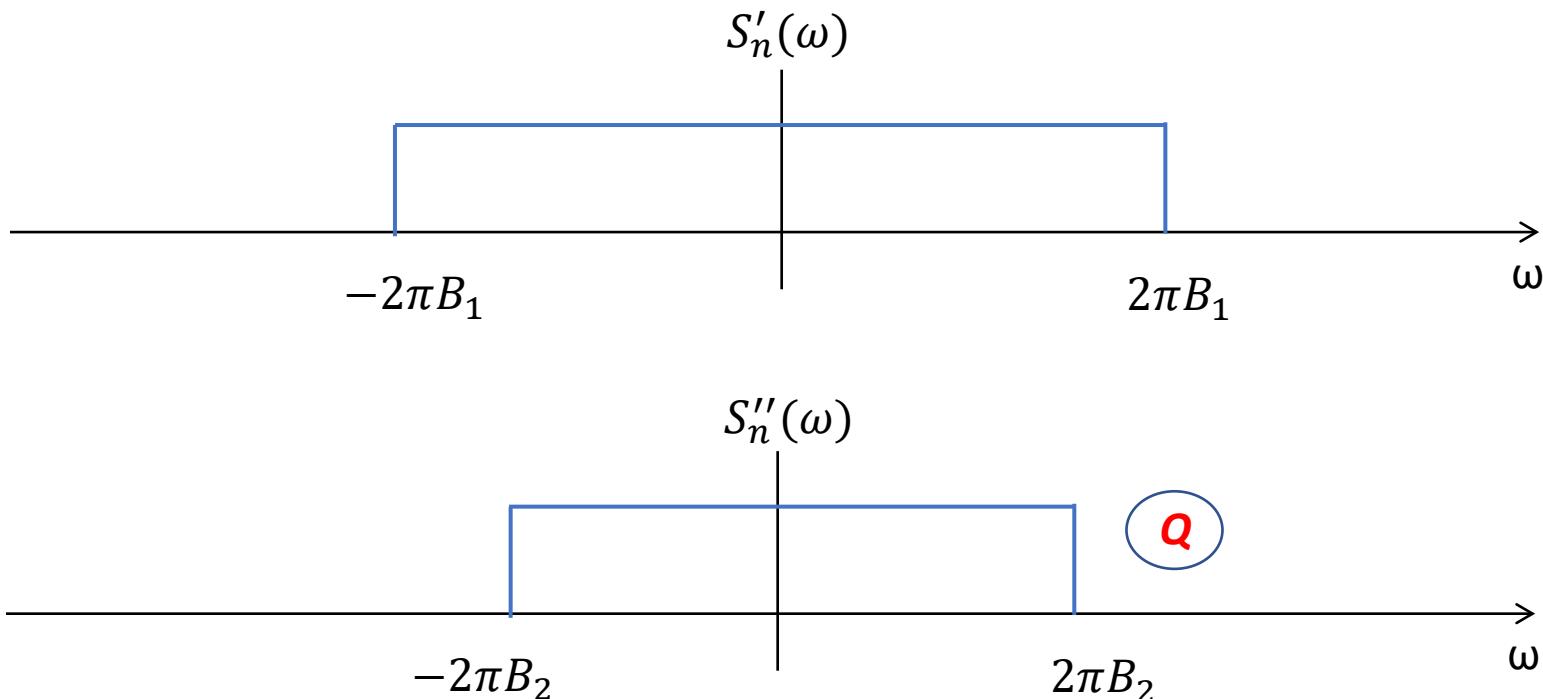
12.1 Electrical Metrology Tools

# 11.0 Typical (Sensor) Measurement Set-up



## 11.1.1 Noise Reduction: Low-pass Filtering

- Low-pass filtering: limits the band of noise from above -> effective with white noise:



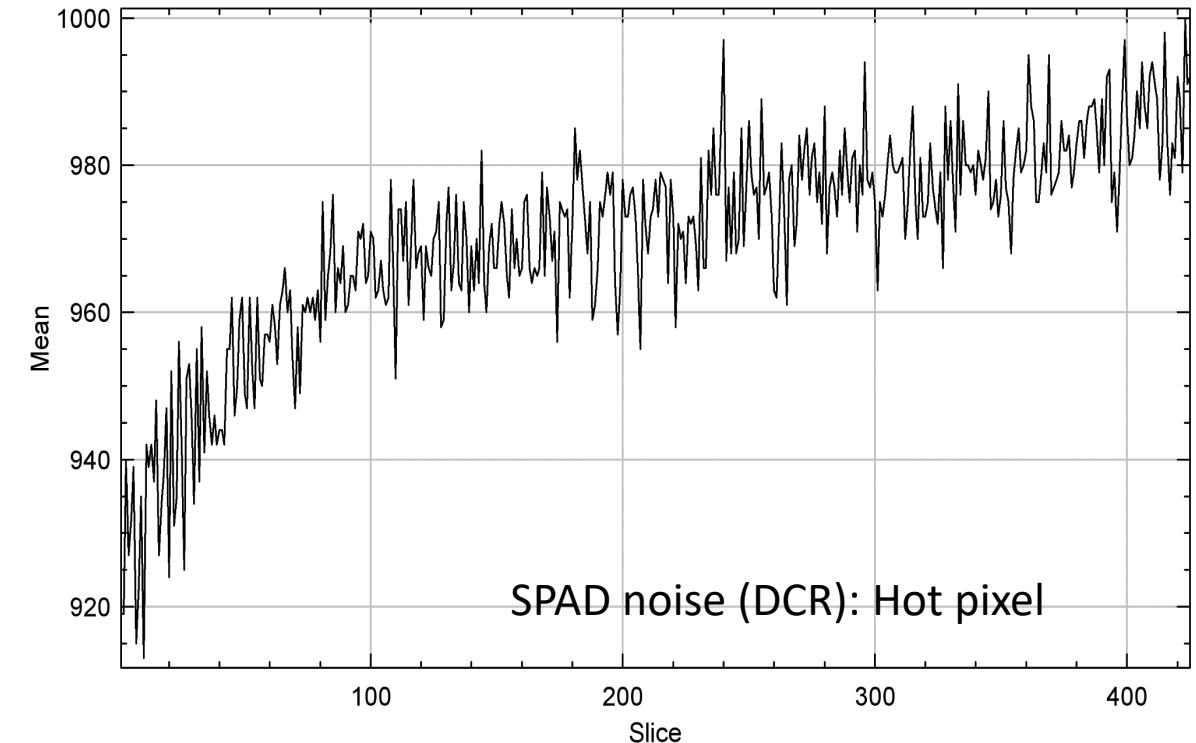
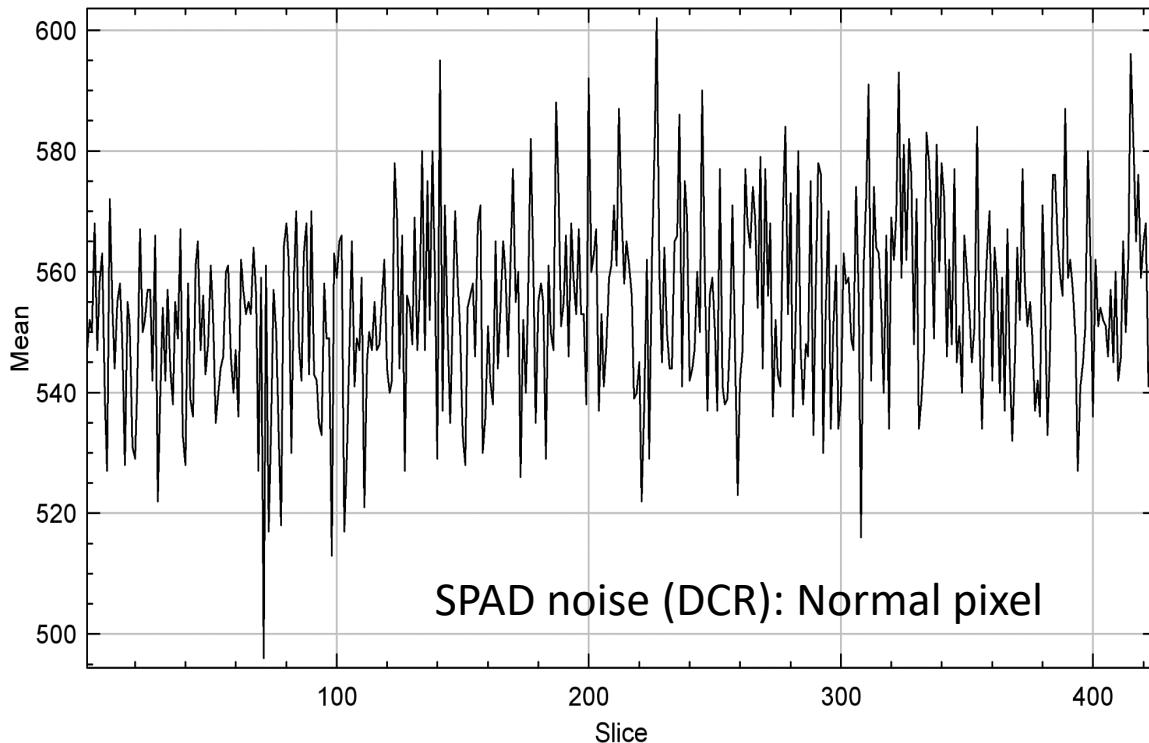
$$\sigma_n^2 = 4kTR \cdot B_2 < 4kTR \cdot B_1$$

where  $B_1 > B_2$

- Obvious, but limits the capability of detecting fast signals, e.g. achieving high frame rates in imaging, or fast transient signals

## 11.1.1 Noise Reduction: Correct for offset and drift

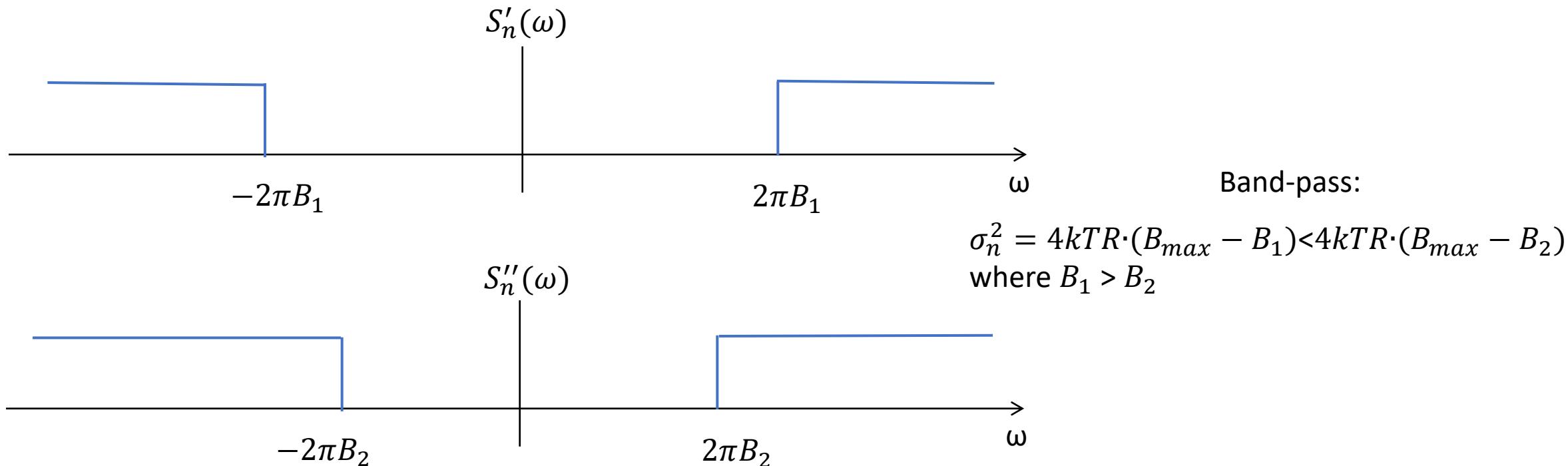
- Eliminate DC component (= offset)
- Same if the offset changes slowly over time (drift), e.g. due to temperature, aging, etc.



Probable cause: thermal drift  
Estimated DAQ time: 9 s

## 11.1.1 Noise Reduction: High-pass/band-pass Filtering

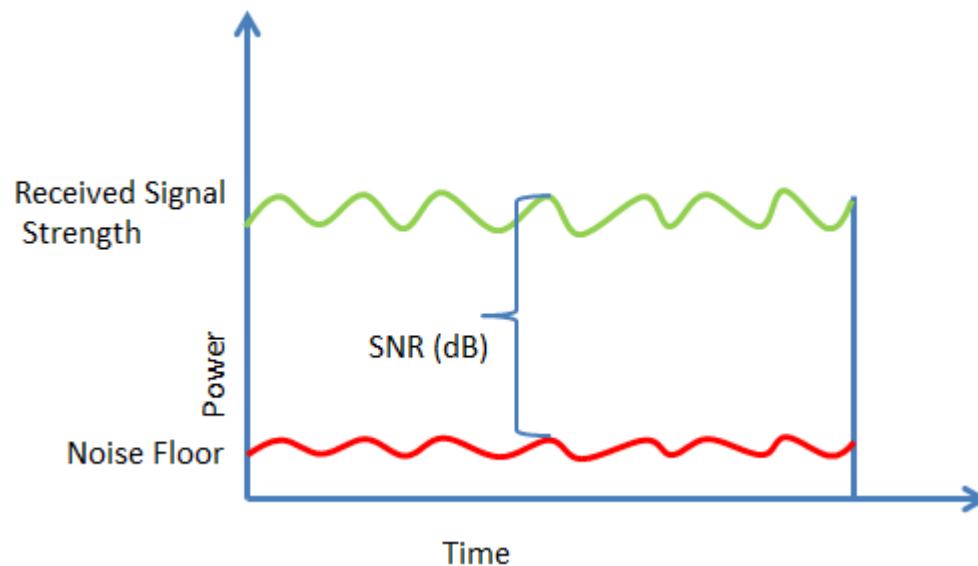
- High-pass filtering: limits the band of noise from below -> effective with white noise:



- HP filter are also effective in reducing noise, as they cut all low frequencies.
- However, they may also eliminate wanted slow signals -> cannot be used in imaging sensors.

## 11.1.2 Noise Reduction: Averaging Techniques

- “Signal averaging is a signal processing technique applied in the time domain, intended to increase the **strength of a signal** relative to **noise** that is obscuring it.”
- “By averaging a set of replicate measurements, the **signal-to-noise ratio (SNR)** will be increased, ideally in proportion to the number of measurements.”



## 11.1.2 Averaging Techniques

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Given a signal  $s(t)$  and noise  $z(t)$ , we assume that:

\*weaker definition of white noise

- Signal  $s(t)$  is **uncorrelated** to noise, and noise  $z(t)$  is **uncorrelated\***.
- Signal power is  $P_{signal} = E\{s^2\}$  and it is **constant** in the replicate measurements.
- Noise is random, with a **mean of zero** and **constant variance** in the replicate measurements:

$$E\{z(t)\} = \mu_{noise} = 0$$

$$Var\{z\} = E\{(z - \mu_{noise})^2\} = E\{z^2\} = P_{noise} = \sigma^2 : \text{Noise Power}$$

## 11.1.2 Averaging Techniques – Noise Power for Sampled Signal

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- Assuming we sample the noise, we get a per-sample variance of

$$Var\{z\} = E\{z^2\} = \sigma^2$$

- However, the noise samples are uncorrelated, therefore (§8.4.5):

$$Var\{N_{avg}\} = Var\left\{\frac{1}{n} \sum_{i=1}^n z_i\right\} = \frac{1}{n^2} Var\left\{\sum_{i=1}^n z_i\right\} = \frac{1}{n^2} \sum_{i=1}^n Var\{z_i\}$$

- Since noise variance is constant ( $\sigma^2$ ):

$$Var\{N_{avg}\} = \frac{1}{n^2} n \sigma^2 = \frac{1}{n} \sigma^2 = \frac{1}{n} P_{noise}$$

-> averaging  $n$  realizations of the same, uncorrelated noise reduces noise power by a factor of  $n$

## 11.1.2 Averaging Techniques – Noise Power for Sampled Signal

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$$Var\{N_{avg}\} = Var\left\{\frac{1}{n} \sum_{i=1}^n z_i\right\} = \frac{1}{n^2} n \sigma^2 = \frac{1}{n} \sigma^2$$

N.B.: The averaging result is also valid when there are different (additive) independent noise sources, e.g. kTC noise and quantization noise, giving rise to independent random processes



Thermal noise? Flicker noise?

### 11.1.3 Signal-to-Noise Ratio (SNR)

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- Define Signal-to-Noise Ratio (SNR) as:

$$SNR = \frac{P_{signal}}{P_{noise}} = \frac{E\{s^2\}}{\sigma^2}$$

$$SNR_{dB} = 10 \log_{10}(SNR) = P_{signal,dB} - P_{noise,dB}$$

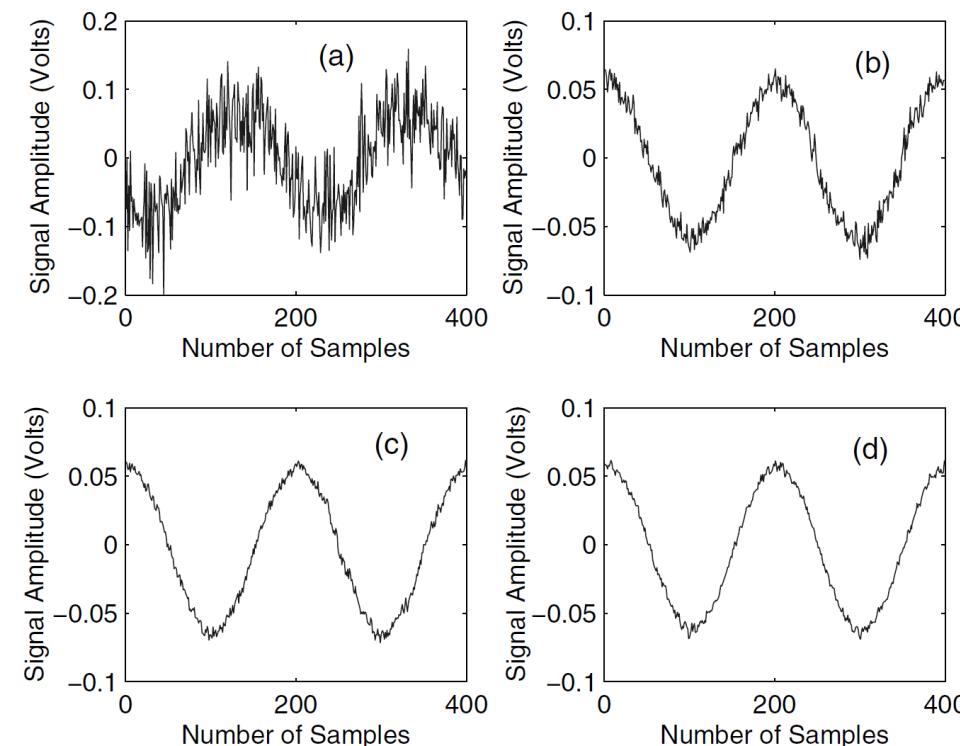
- Measure both signal and noise within the same system bandwidth. The SNR matters, rather than the absolute signal strength!
- SNR>1 (0 dB) means more signal than noise

NB: SNR can be measured w.r.to power or amplitude!

$$SNR_{dB} = 10 \log_{10} \left[ \left( \frac{A_{signal}}{A_{noise}} \right)^2 \right] = 20 \log_{10} \left( \frac{A_{signal}}{A_{noise}} \right) = A_{signal,dB} - A_{noise,dB}$$

## 11.1.4 Averaging Techniques – Signal power for sampled signals

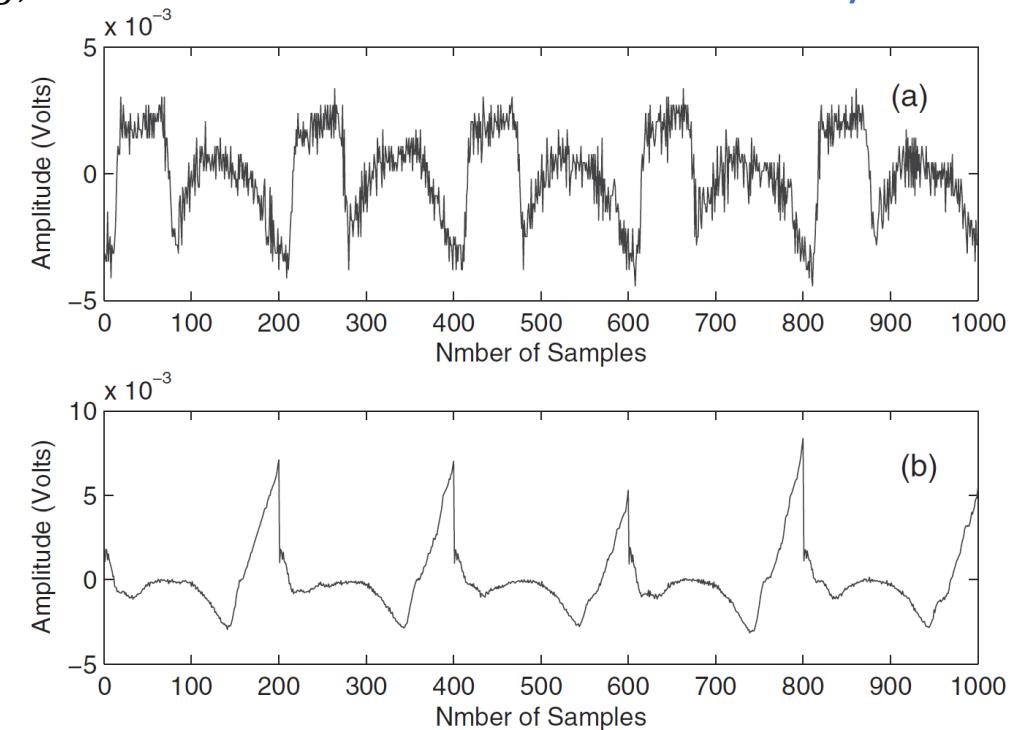
- In the case of a constant or repetitive signal, averaging allows us to increase the SNR as follows:



$$SNR_{avg, identical\ signals} = \frac{P_{avg, identical\ signals}}{P_{avg, noise}} = n \ SNR$$

-> signal adds coherently, noise incoherently

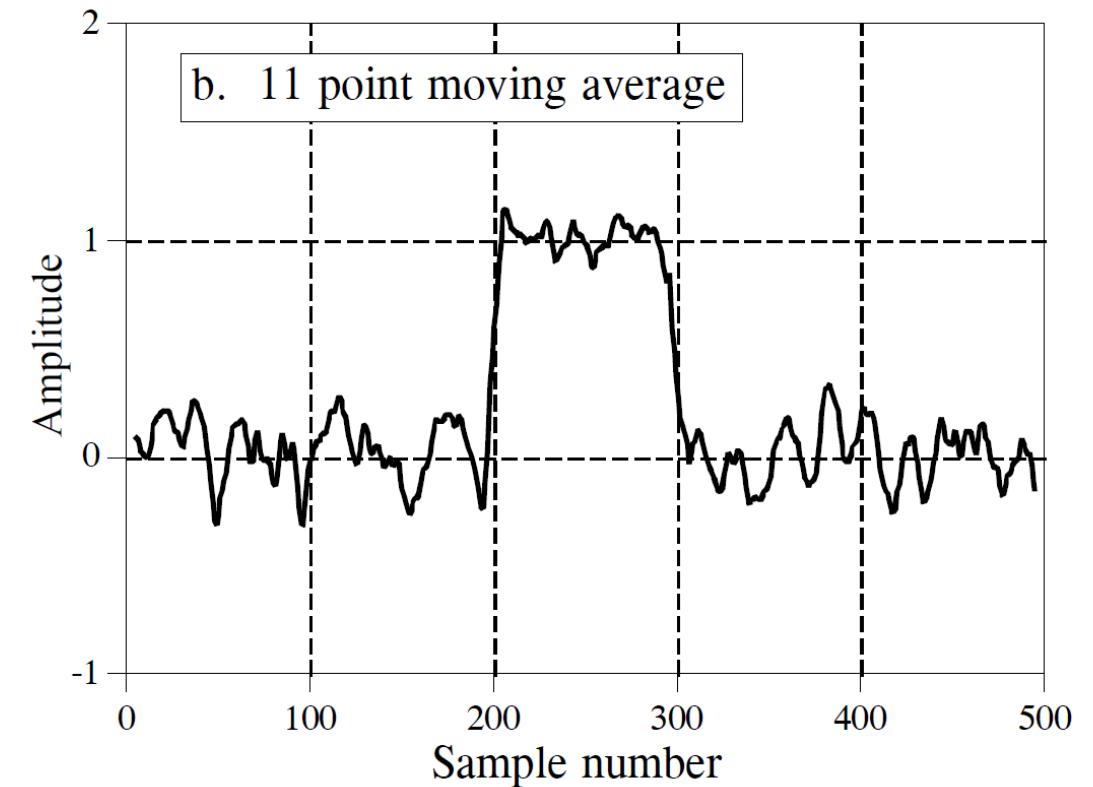
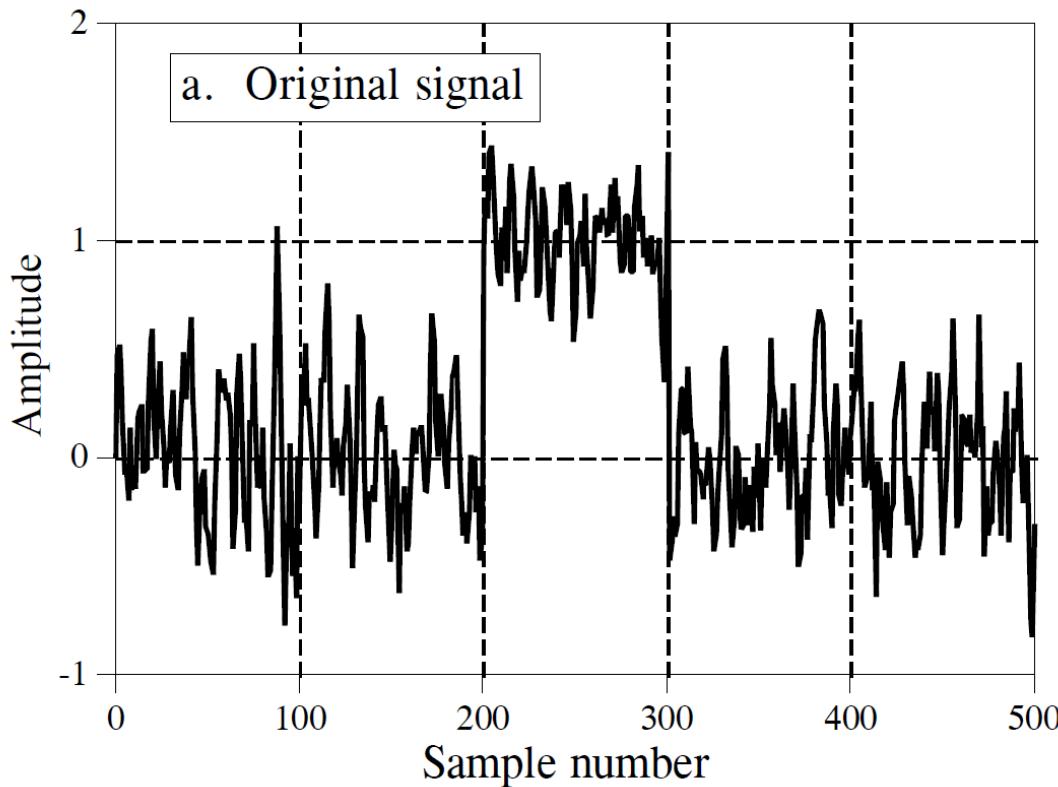
Repetitive signal



ECG signal, baseline-corrected before vs. after averaging  
(NB: home-made – still some work to do ☺)

## 11.1.4 Averaging Techniques – Signal power for sampled signals

- Constant signal -> Example: Moving average filter



NB: decreases the amplitude of the random noise (good), but also reduces the sharpness of the edges (bad) (very good smoothing filter – time domain action – but very bad low-pass filter – frequency domain action).

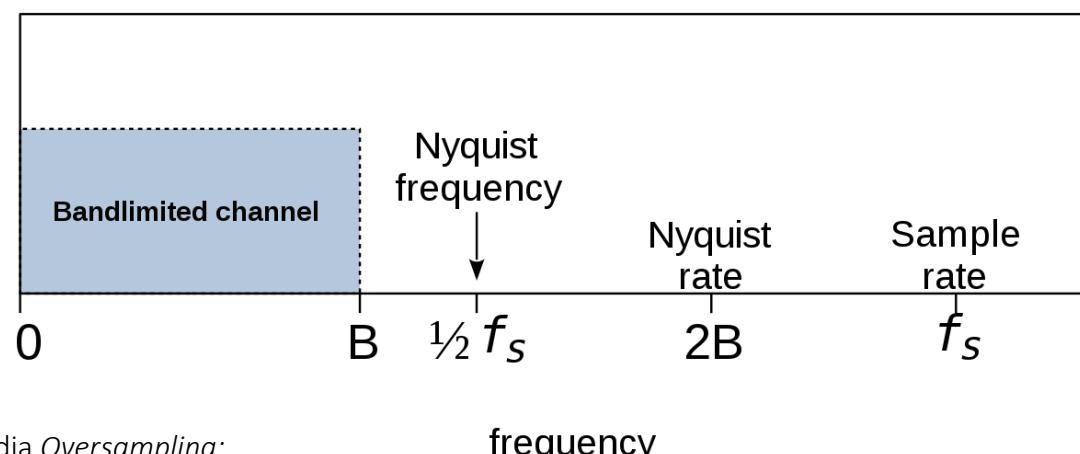
## 11.1.4 Averaging Techniques – Signal power for sampled signals

- Constant signal -> Employ Oversampling

Oversampling = sampling at higher than the Nyquist rate\* =  
2x highest frequency component of a bandwidth-limited signal

- Rationale: the observed signal is correlated since oversampling simply implies that the signal observations are strongly correlated
- NB: Oversampling can be helpful in avoiding aliasing by relaxing anti-aliasing filter performance requirements (without oversampling, it is very difficult to implement filters with the sharp cutoff necessary to maximize use of the available bandwidth)

Relationship of Nyquist frequency & rate (example)

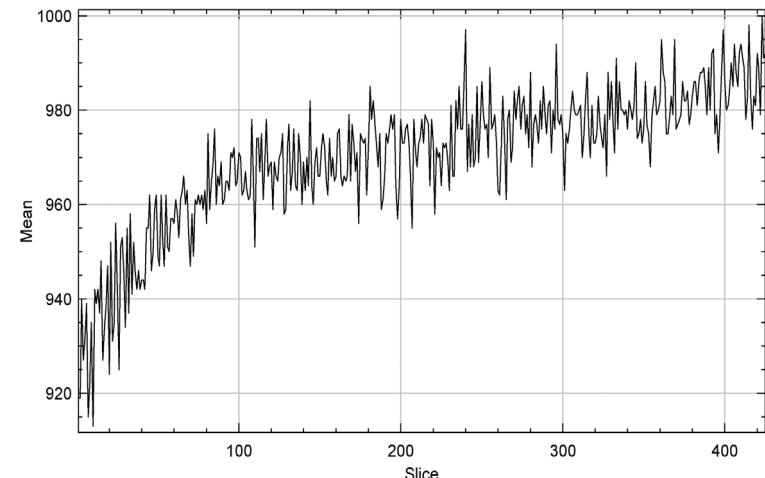


\*which is not the Nyquist frequency (= half the sampling rate)!

By Bob K - Own work, CC0, <https://commons.wikimedia.org/w/index.php?curid=94674142>

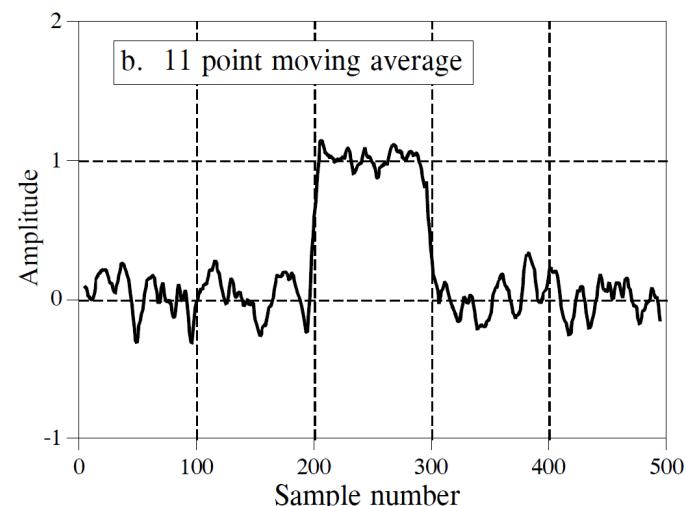
# Take-home Messages/W11-1

- *Noise Reduction:*
  - Low-pass filtering, offset and drift correction
  - High-pass/Bandpass filtering
  - Averaging Techniques
    - Underlying conditions and noise power reduction
      - Independent noise sources
    - Signal-to-Noise ratio and its improvement
    - Filtering examples, oversampling



$$Var\{N_{avg}\} = \frac{1}{n} P_{noise}$$

$$SNR = \frac{P_{signal}}{P_{noise}} = \frac{E\{s^2\}}{\sigma^2}$$



# Outline

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10.1 Charges, Currents, and Voltages

10.2 Noise Background

10.3 Noise Sources

11.1 Noise Reduction, Averaging Techniques

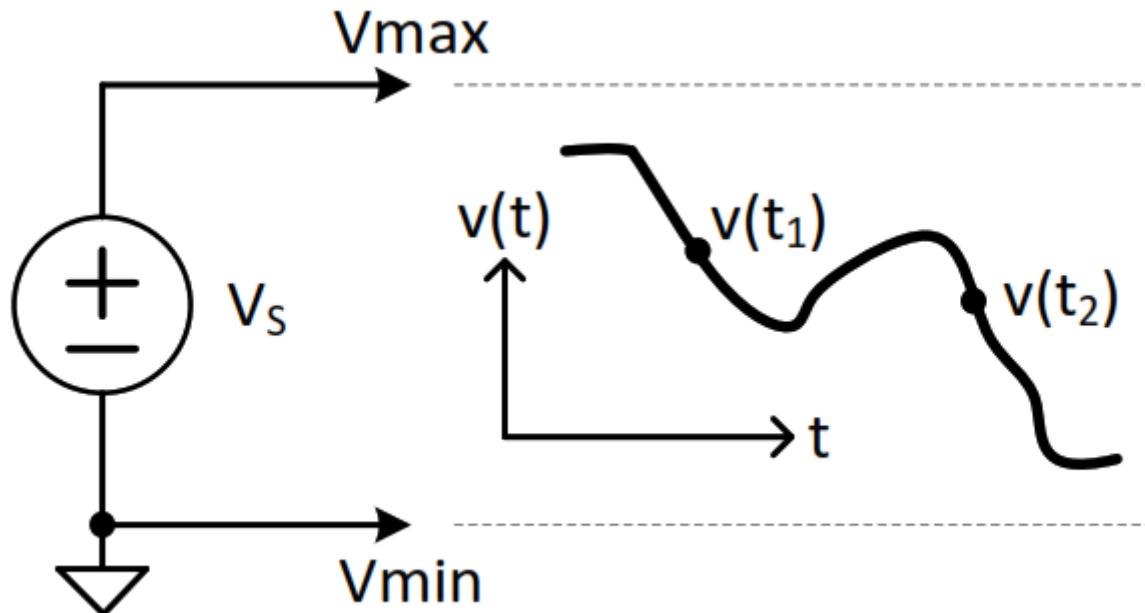
11.2 **Electric Signals, Analog-to-Digital Conversion**

11.3 Timing – Time-to-Digital Conversion

12.1 Electrical Metrology Tools

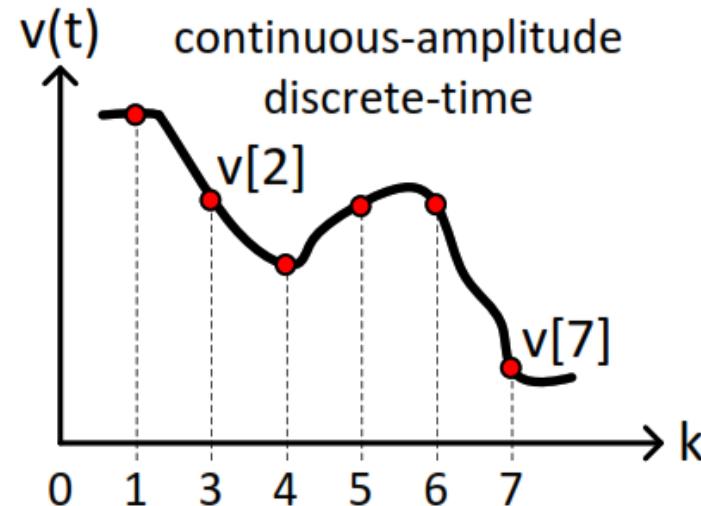
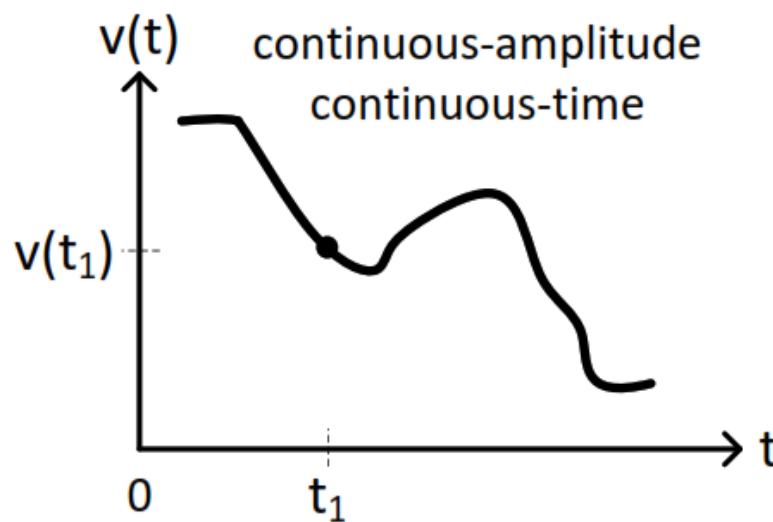
## 11.2.1 Electric Signals

- Electrical signal typically encodes the information as a voltage level  $v(t)$  versus time  $t$ .
- Sometimes it could be a current level  $i(t)$  or charge level  $q(t)$ .



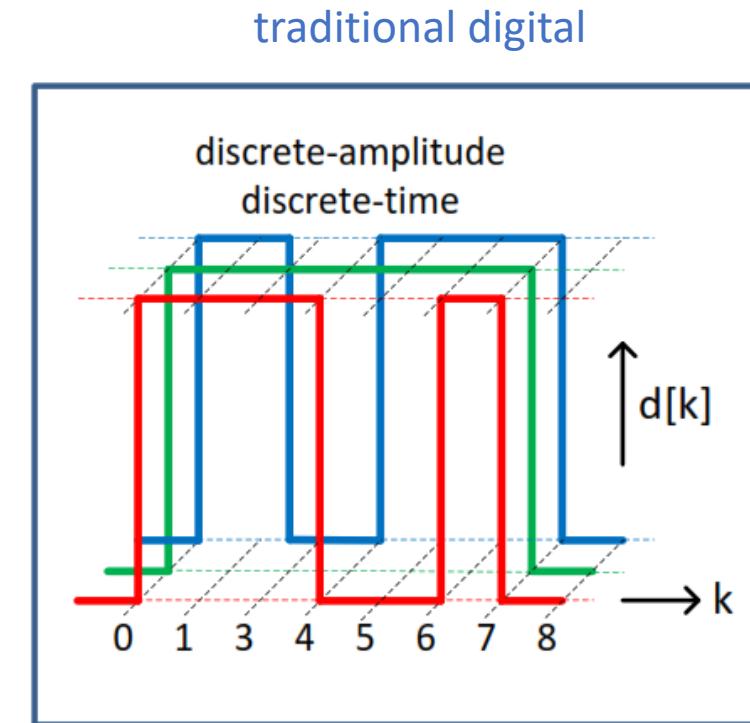
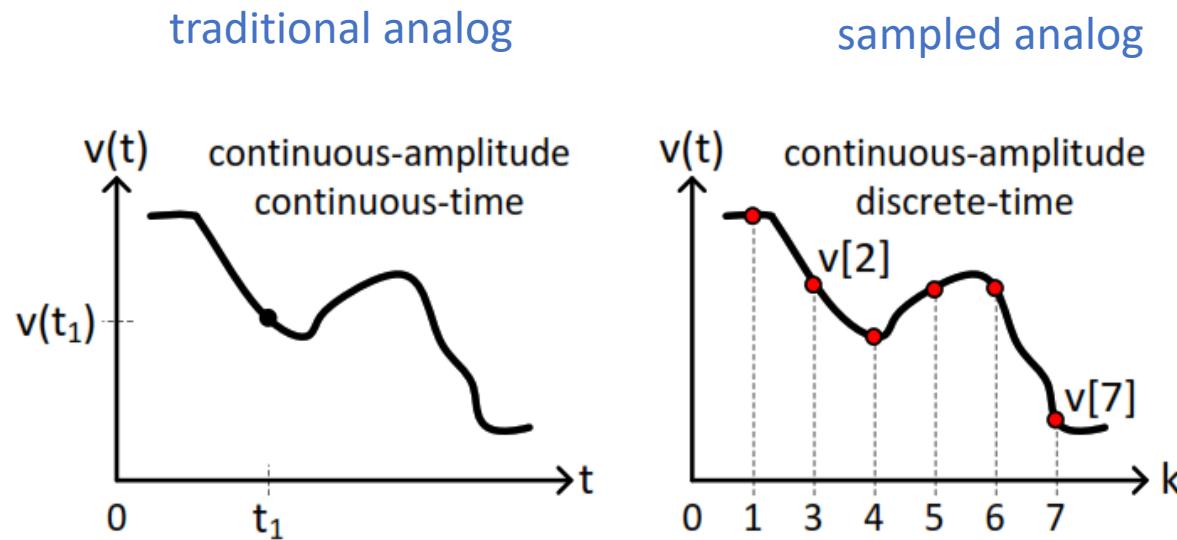
## 11.2.1 Electric Signals

- Analog signal amplitude is continuous
- Analog signal time can be continuous or discretized
- Discretization in time involves sampling methods (impulse, zero-order hold, sampled integration, etc.)



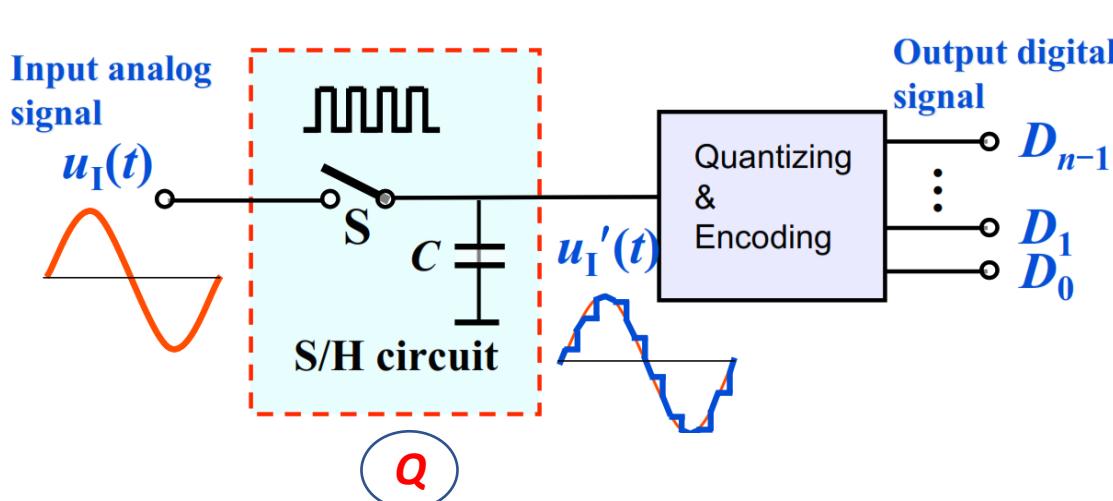
## 11.2.1 Electric Signals

- Digital signals quantize  $v(t)$  into two levels (logic HIGH and logic LOW) and use an array of them
- Synchronous digital circuits use clocks, hence  $d[k]$  is a digital bit or word value at a discrete-time index.



## 11.2.2 Analog to Digital Converter (ADC)

- ADC provides a link between the **analog world** of transducers and the **digital world** of signal processing and data handling.
- ADCs are used virtually everywhere where an analog signal has to be **processed, stored** or **transported** in digital form.
- Some examples of ADC usage are digital **voltmeters**, **cell phone**, **thermocouples**, and digital **oscilloscopes**.



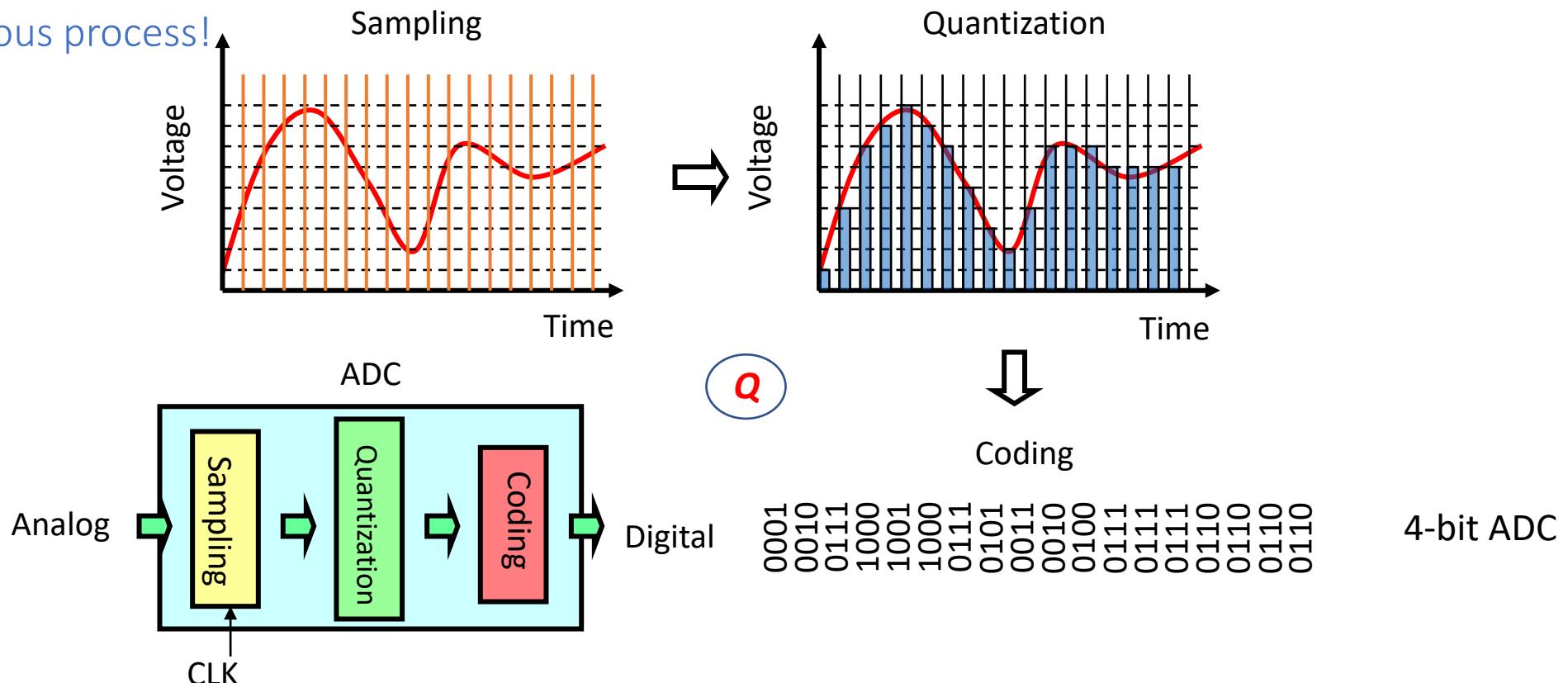
Two-step process:

1. Sampling and Holding (S/H)
2. Quantizing and Encoding (Q/E)

S/H: hold the input value constant during the time needed for a conversion (*conversion time*)

## 11.2.2 Analog to Digital Converter (ADC)

- An ADC (analog-to-digital converter) samples a **voltage**, a **charge**, or a **current** at **discrete times** and **quantizes** it (quantization in time and signal).
- **Synchronous process!**



## 11.2.2 ADC – Ideal Case

- Resolution or LSB:

The smallest change in analog signal that will result in a change in the digital output.

$$\Delta V = \frac{V_r}{2^N}$$

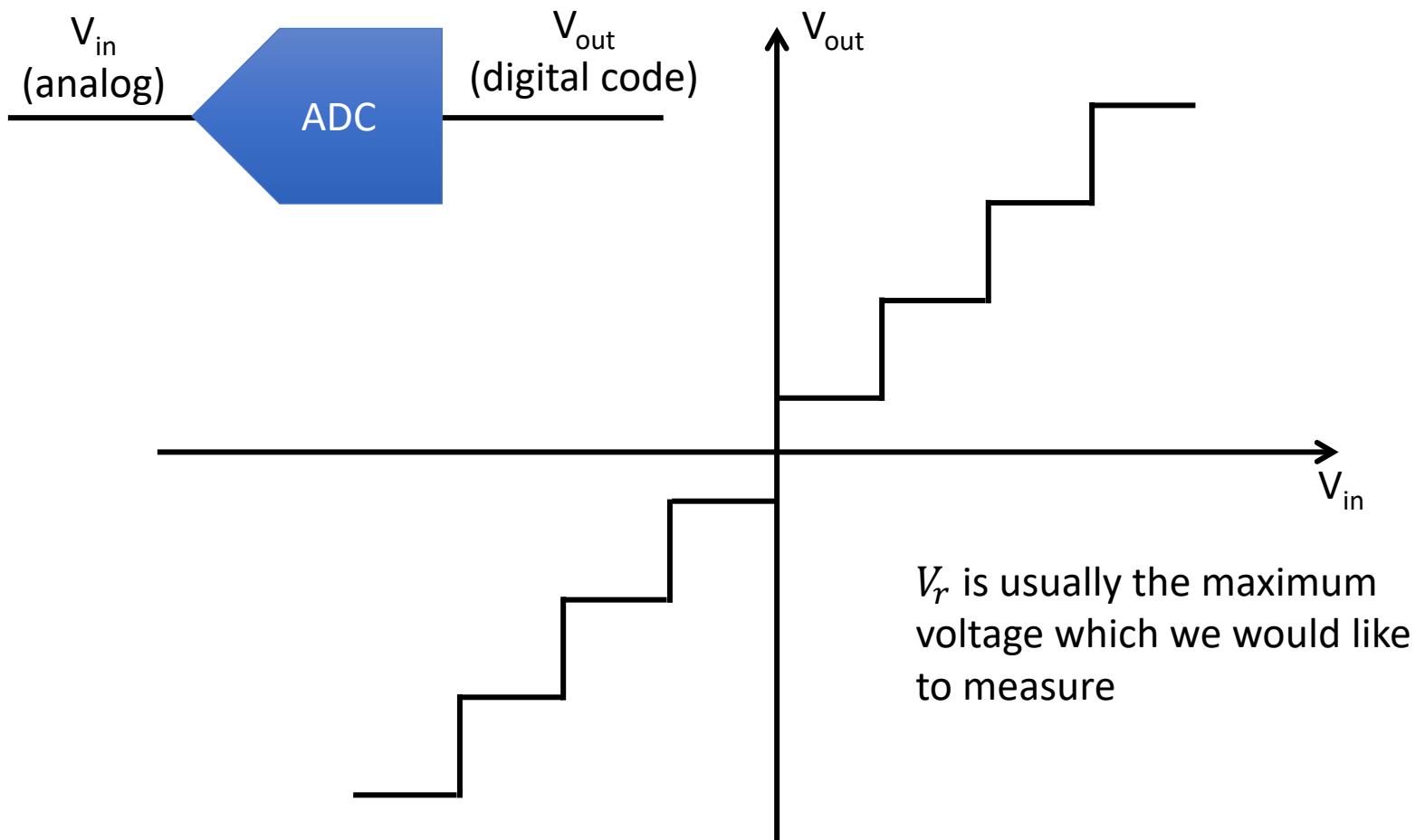
Q

$V_r$  = Reference Voltage Level

N = # of bits

$2^N$  = # of states

$\Delta V$  = Resolution



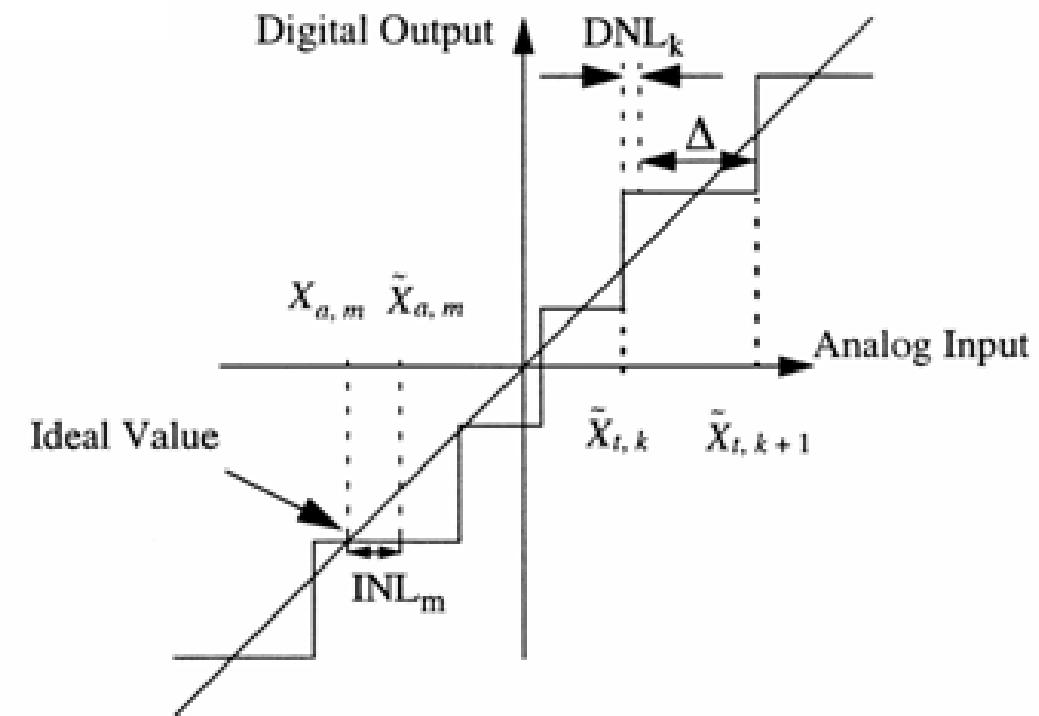
## 11.2.2 ADC – Real Case

- Non-idealities:
  - Differential non-linearity (DNL)
  - Integral non-linearity (INL)

$$DNL_j \equiv \frac{Width_{ACTUAL,j} - Width_{IDEAL}}{Width_{IDEAL}}$$

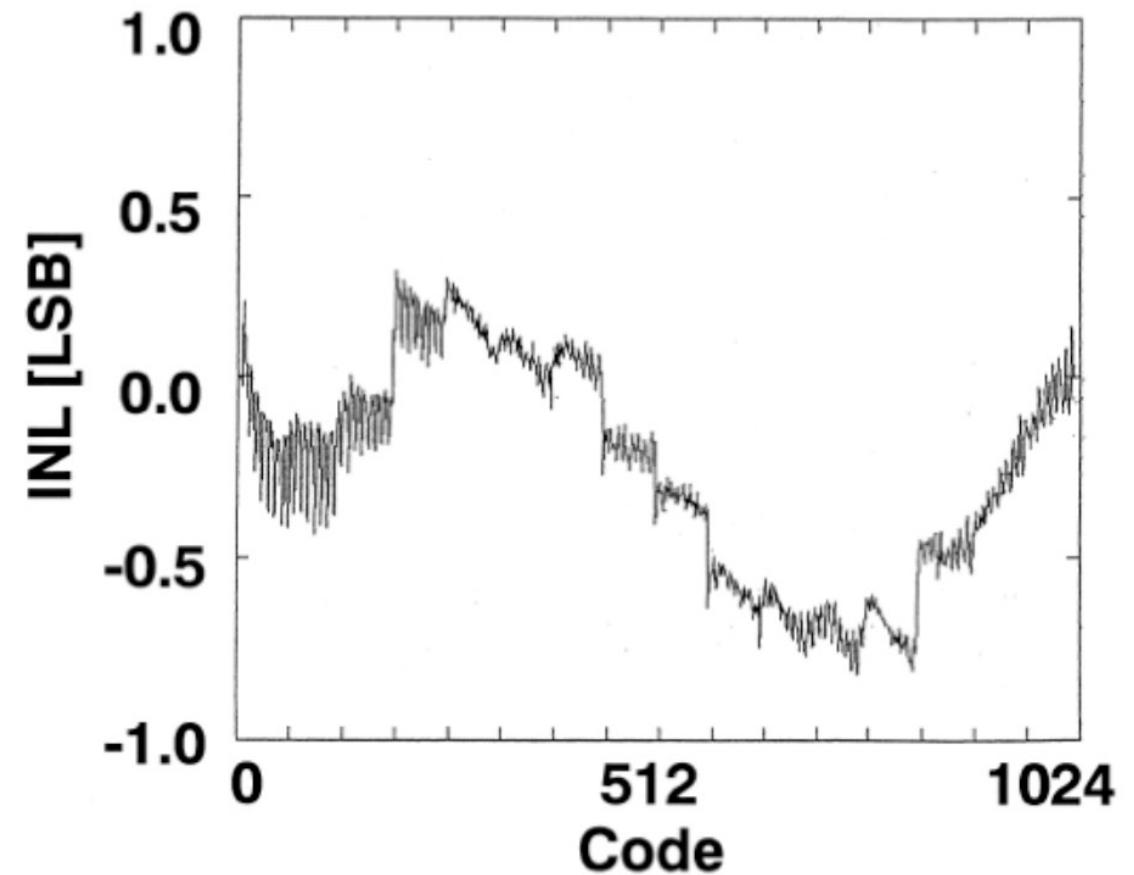
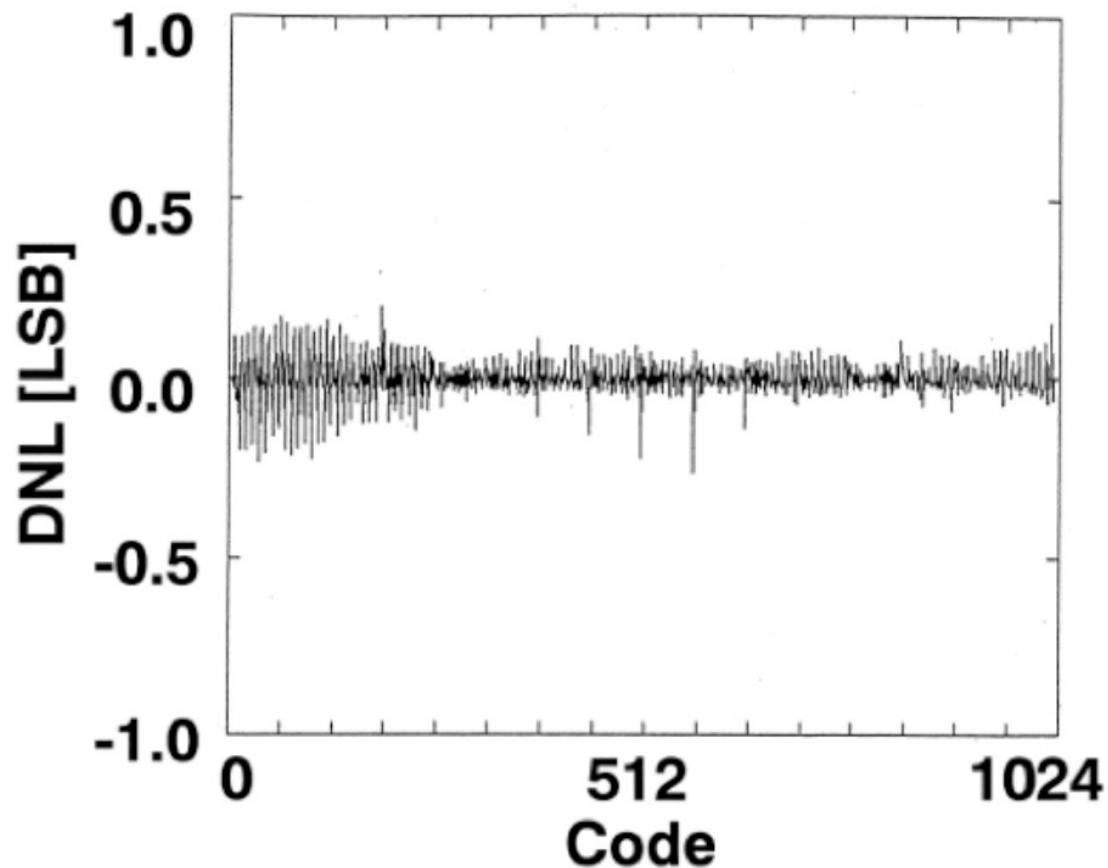
$$INL_j = \sum_{k=0}^{k=j} DNL_k$$

$$DNL_j = INL_{j+1} - INL_j$$



INL = deviation of transfer curve from ideal (linear)

## 11.2.2 ADC – Real Case, Example

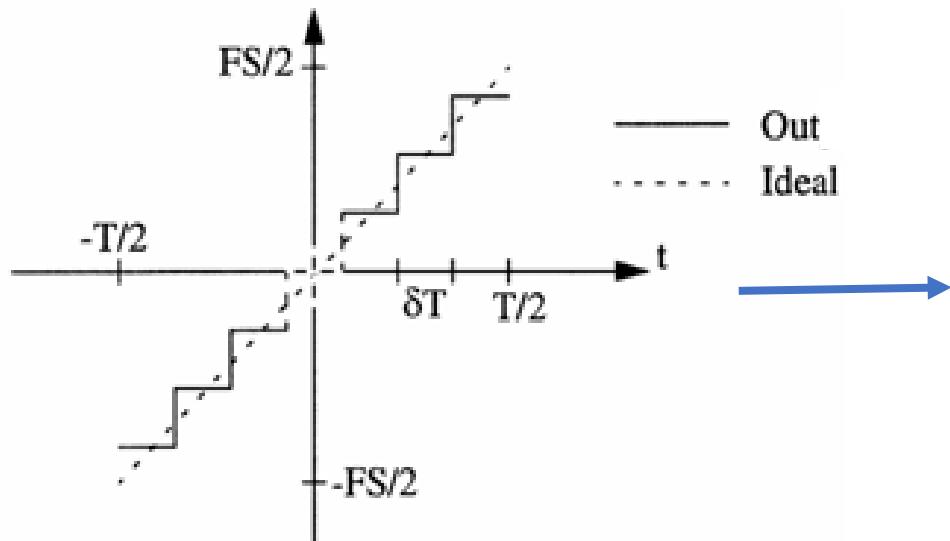


Q

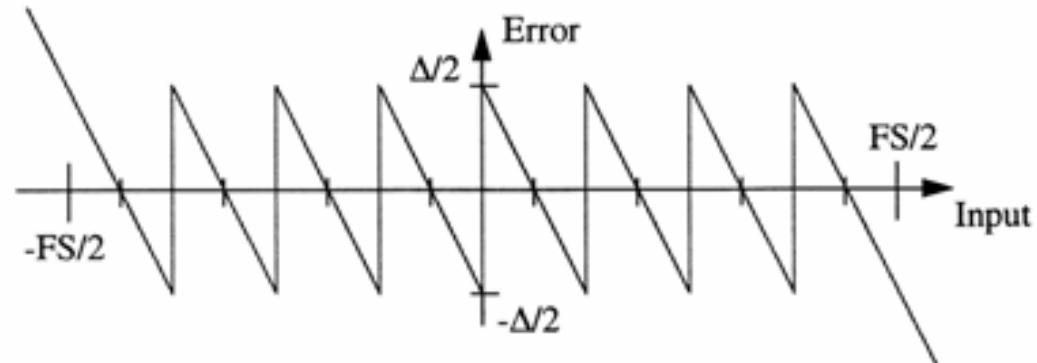
Source: A. Matzusawa

## 11.2.2 ADC – Quantization Noise

Transfer characteristics



Quantization noise



(error = Out-In)

$$\sigma_{noise}^2 = P_{noise} = \int_{-\Delta/2}^{\Delta/2} e^2 P_U(e) de = \int_{-\Delta/2}^{\Delta/2} e^2 \frac{1}{\Delta} de = \frac{\Delta^2}{12}$$

Uniform distribution  
(ideal ADC)!

$$PDF: P_U(e) = \begin{cases} \frac{1}{\Delta}, & |e| < \frac{\Delta}{2} \\ 0, & \text{otherwise} \end{cases}$$

See also W9 3.0.1

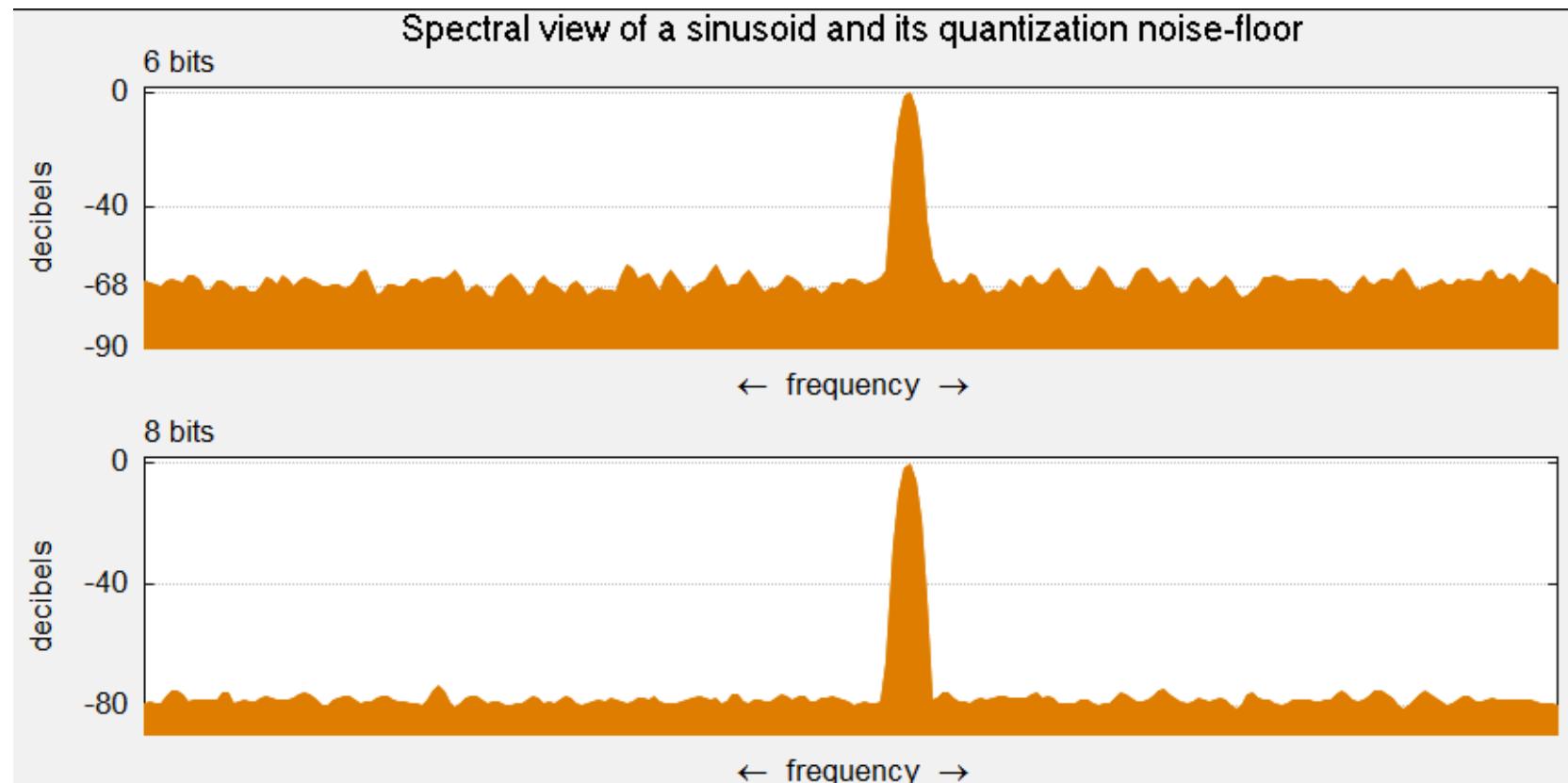
## 11.2.2 ADC – Quantization Noise vs. Oversampling

- Signal-to-quantization-noise ratio (SQNR):

$$SQNR = 20 \log_{10}(2^Q) = 6.02 \cdot Q + 1.76 \text{ dB, } Q = \# \text{ of quantization bits}$$

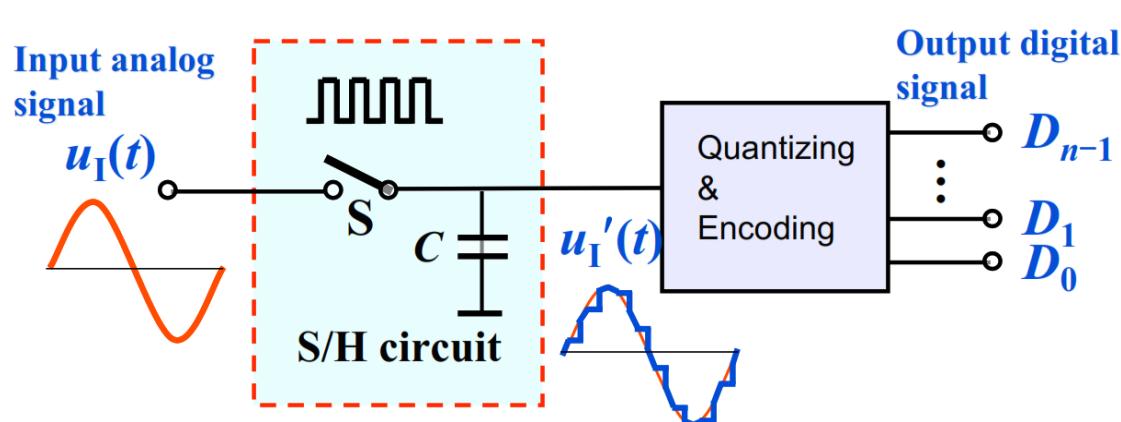
64 levels (6 bits) vs. 256 levels (8 bits) -> measurable difference in the noise floors

- Is distributed from 0 to the Nyquist frequency (= half the sampling rate)
- *In addition:* if part of the ADC's bandwidth is not used, as is the case with oversampling, some of the quantization error will occur out-of-band, effectively improving the SQNR for the bandwidth in use.



## 11.2.2 ADC – Quantization Noise

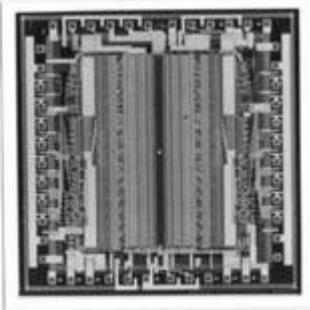
- Example of oversampling application: audio frequency ADCs
- Q: sampling of a constant signal -> do I only have quantization noise? 



-> in practice no, because of kTC (thermal) noise intrinsic in the S/H process!

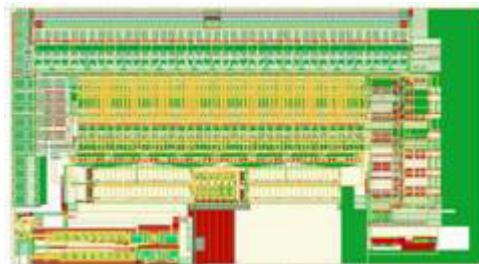
## 11.2.2 ADC in CMOS

Matsuzawa, ISSCC 1991



6b, 1GHz ADC  
2W  
1.5um Bipolar

Sushihara, et al, ISSCC 2000



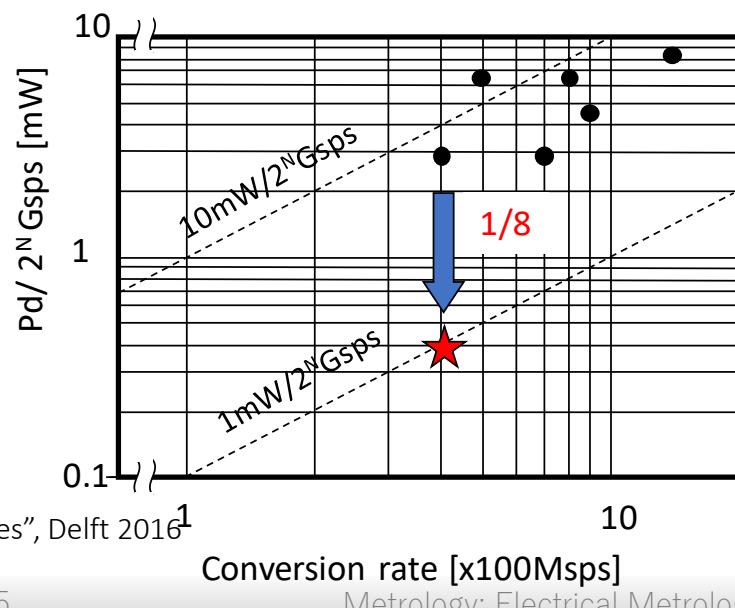
6b, 800MHz ADC  
400mW, 2mm<sup>2</sup>  
0.25um CMOS  
Pd of high speed CMOS ADCs

Sushihara and Matsuzawa, ISSCC 2002

World lowest Pd HS ADC



7b, 400MHz ADC  
50mW, 0.3mm<sup>2</sup>  
0.18um CMOS



Pd = power dissipation. Horizontal = conversion rate.  
Power per bit normalized in units of Gsps.

Source: A. Matzusawa



E. Charbon, "Image Sensors – ET 4390 Course Slides", Delft 2016

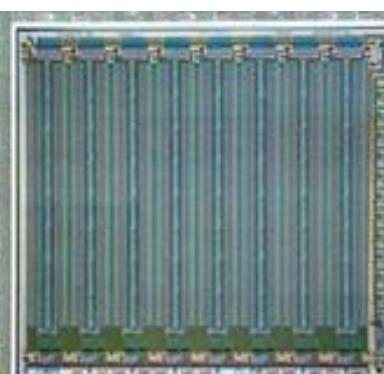
## 11.2.2 30 Years of ADC Progress

- Improvements in the last 20 years:

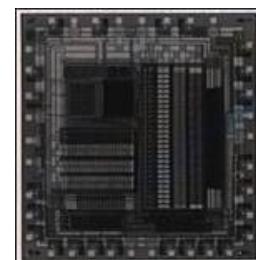
$1/2000 \times \text{power}$   $1/200,000 \times \text{cost}$

1980	1982	1993	2006
Conventional product	World 1 <sup>st</sup> Monolithic	World lowest power	SoC Core
Board Level (Disc.+Bip)	Bipolar (3um)	CMOS (1.2um)	CMOS (0.15um)
20W	2W	30mW	10mW
\$ 8,000	\$ 800	\$ 2.00	\$ 0.04

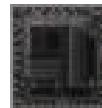




T. Takemoto and A. Matsuzawa,  
JSC, pp.1133-1138, 1982.



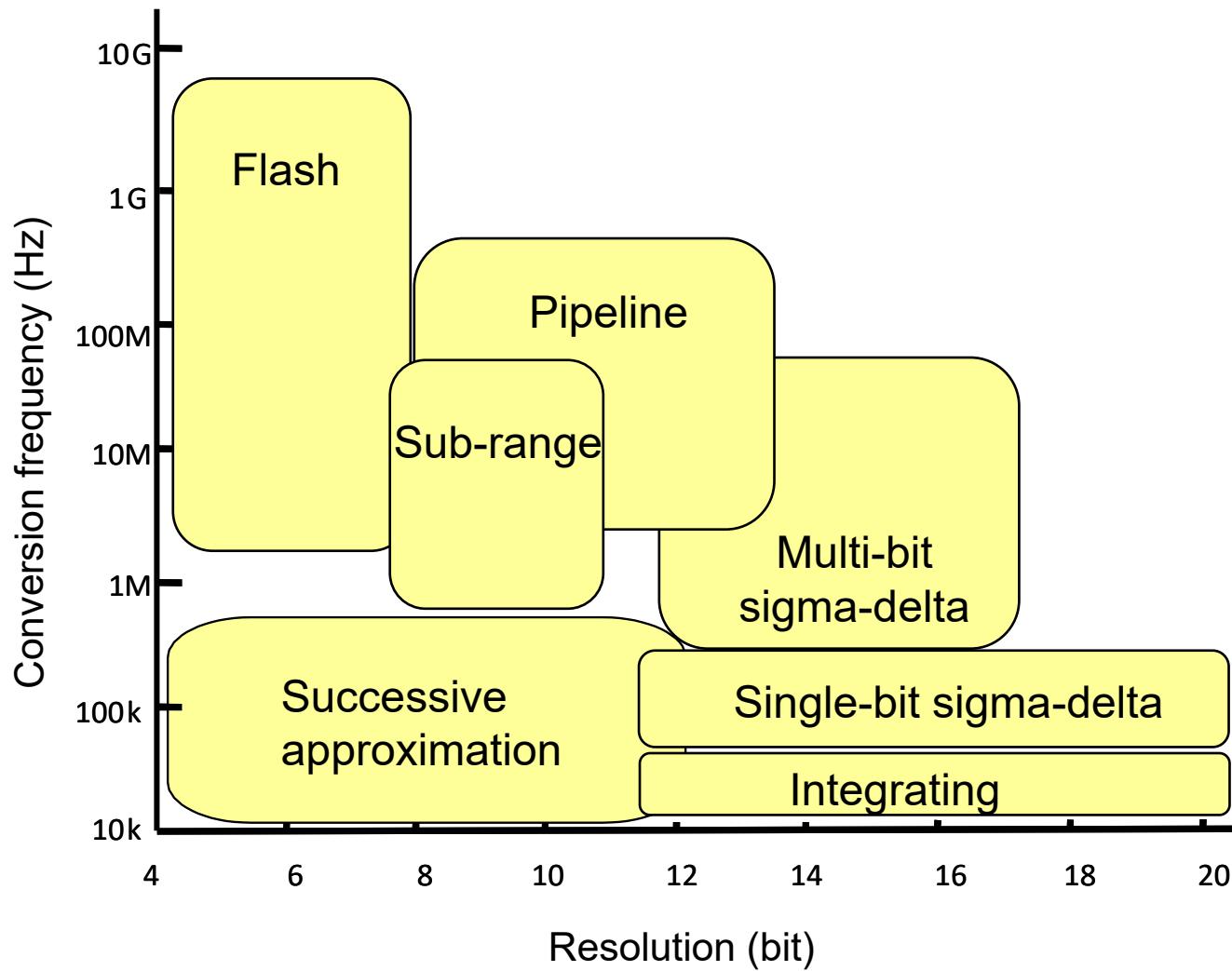
K. Kusumoto and A. Matsuzawa,  
ISSCC 1993.



Q

Source: A. Matsuzawa

## 11.2.2 ADC - Architectures

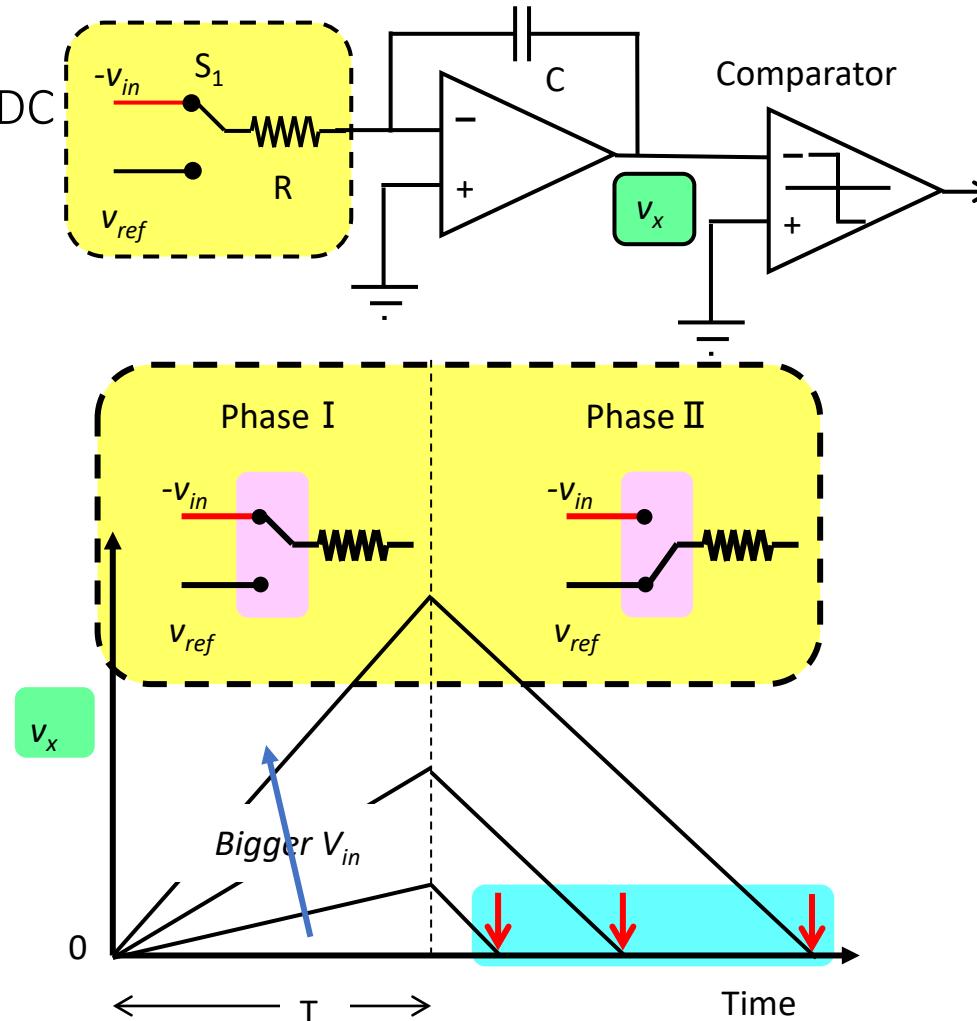


## 11.2.2 Integrating ADC

- Perhaps the most frequently used ADC
- Slow but high resolution
- Used for example in voltmeters

### Features:

- High resolution (<20b)
- Low speed
- Small DNL
- Can implement zero offset voltage
- Small area



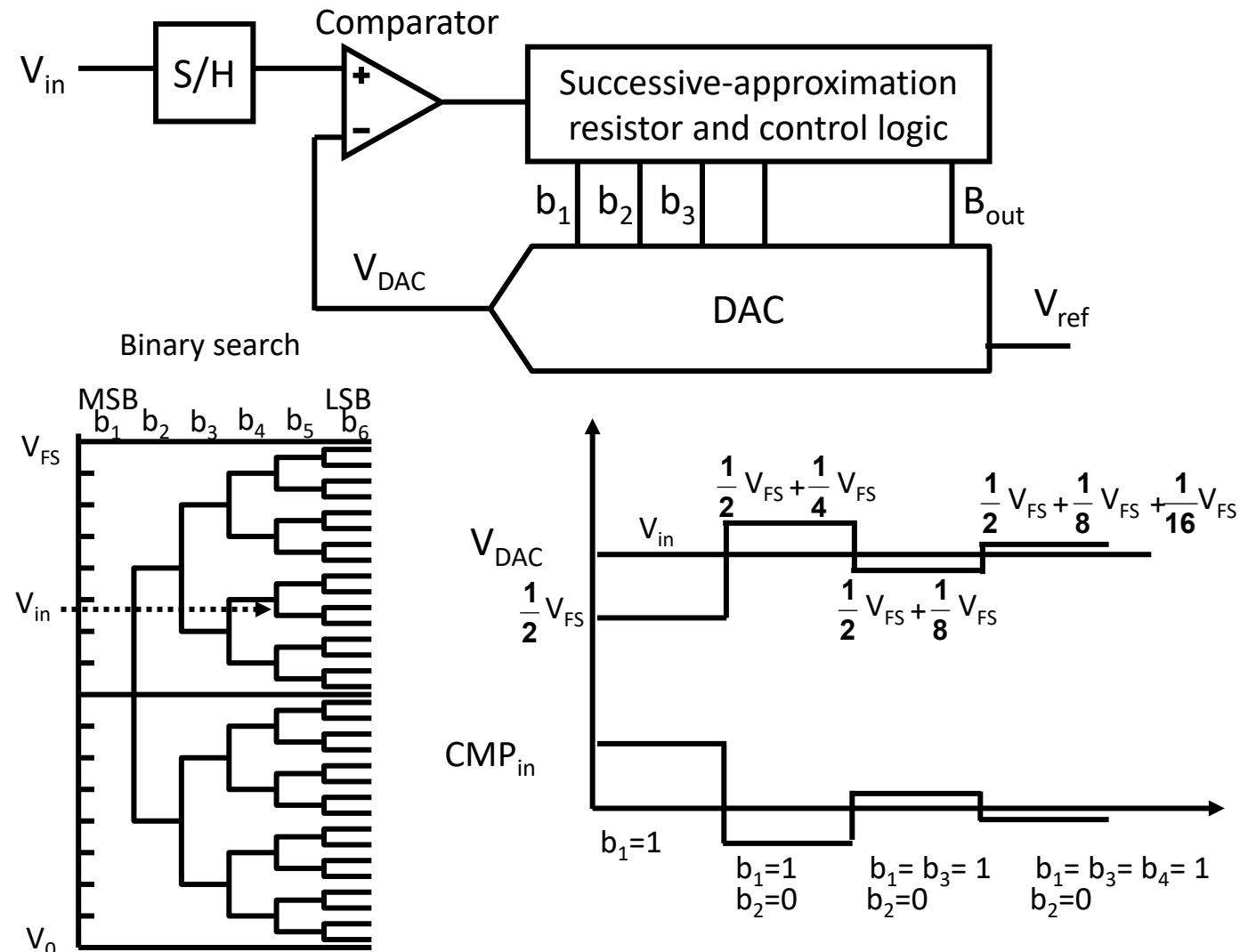
Integrating OpAmp with capacitive feedback – charge capacitor in phase 1, discharge in phase 2 (opposite polarity), and measure the time until complete discharge ( $v_{ref} = 0$ ).

Concept: A. Matzusawa

$$V_x(T) = \int_0^T \frac{-V_{in}}{RC} d\tau = \frac{V_{in}}{RC} T$$

## 11.2.2 Successive-Approximation ADC

- Uses a n-bit DAC to compare DAC and original analog results.
- Successive Approximation Register (SAR) supplies an approximate digital code of  $V_{in}$  to DAC.
- Comparison changes digital output to bring it closer to the input value.
- Uses Close-loop Feedback Conversion.
- n cycles are needed for n bits



## 11.2.2 Successive-Approximation ADC

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### Advantages

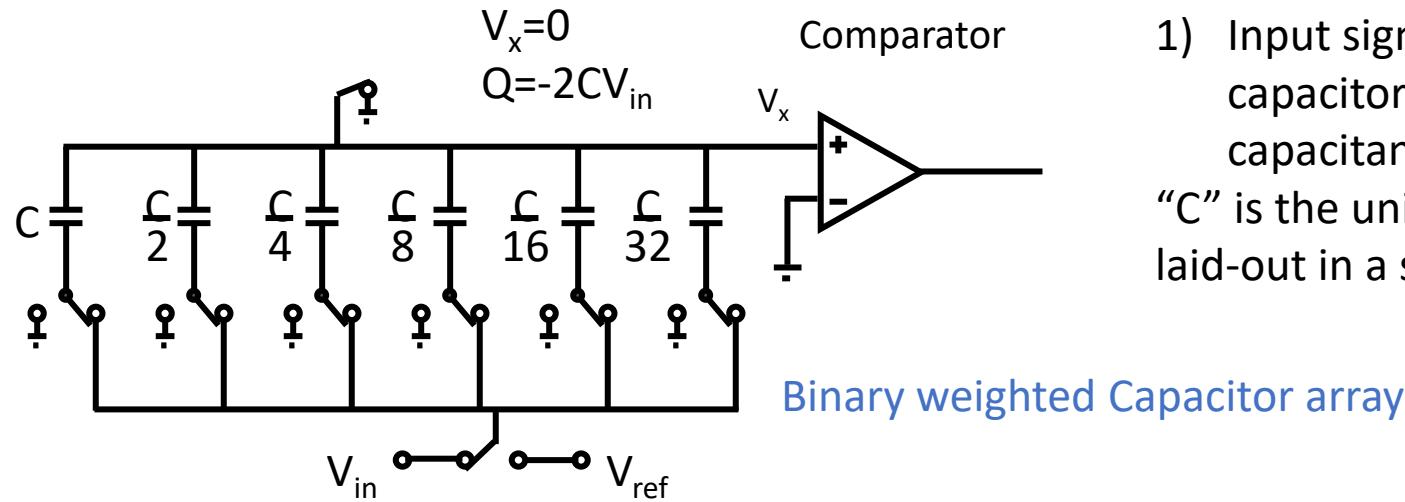
- Capable of high speed and reliable
- Medium accuracy compared to other ADC types
- Good trade-off between speed and cost
- Capable of outputting the binary number in serial format
- Conversion time independent of amplitude of  $V_{in}$

### Disadvantages

- Higher resolution successive approximation ADCs will be slower
- Speed limited to  $\sim 5$  Msps

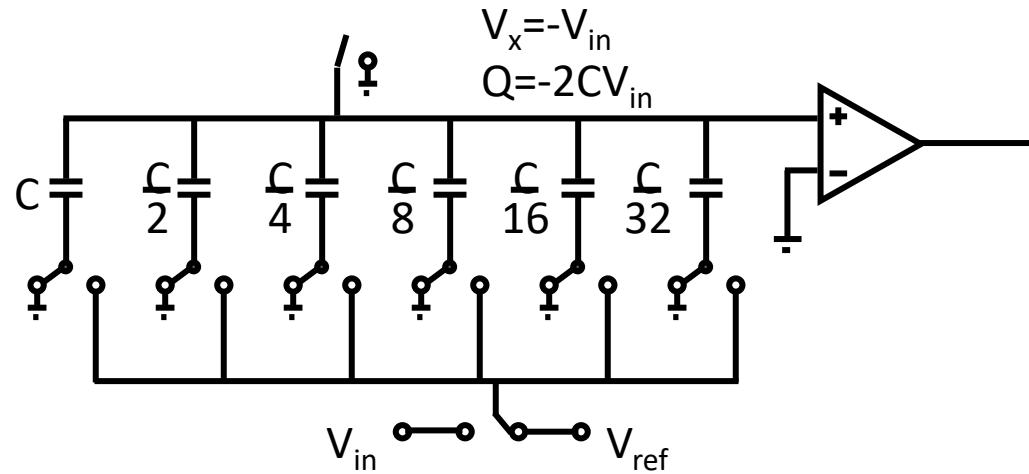
## 11.2.2 Charge-redistribution ADC

### 1) Sampling



- 1) Input signal is stored on a capacitor bank with a total capacitance value of  $2C$ . “C” is the unit capacitor and is laid-out in a standardized manner.

### 2) Hold

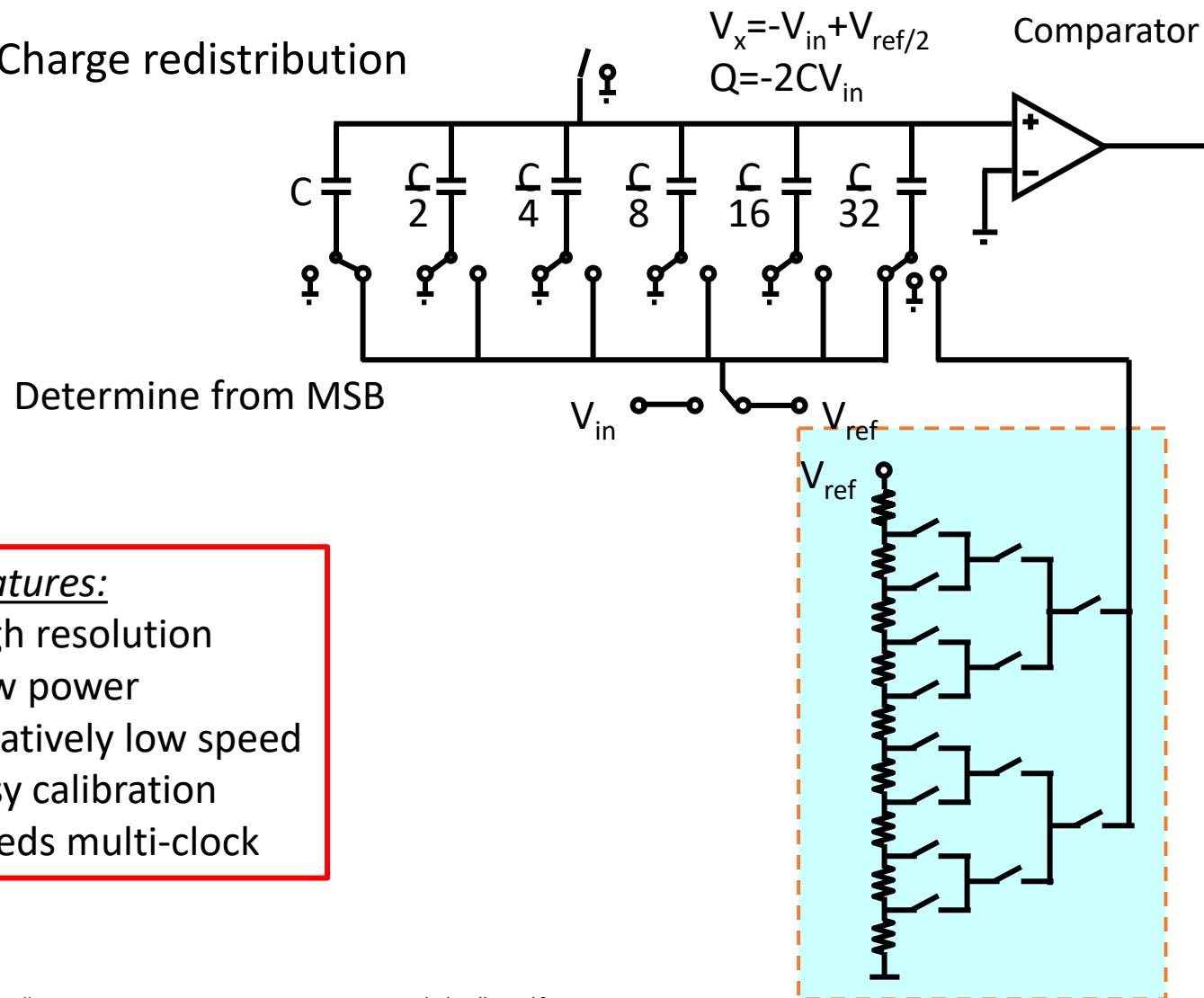


- 2) NB: can not hold the charge indefinitely!

Source: A. Matzusawa

## 11.2.2 Charge-redistribution ADC

### 3) Charge redistribution



Features:

- High resolution
- Low power
- Relatively low speed
- Easy calibration
- Needs multi-clock

3) The ground plates of the capacitors are switched one after the other from ground to the reference voltage. Depending on the original value of the input voltage, the comparator will decide to keep the MSB switch in this position or return to ground. Every bit is subsequently tested.

If needed

Resistor ladder for higher resolution

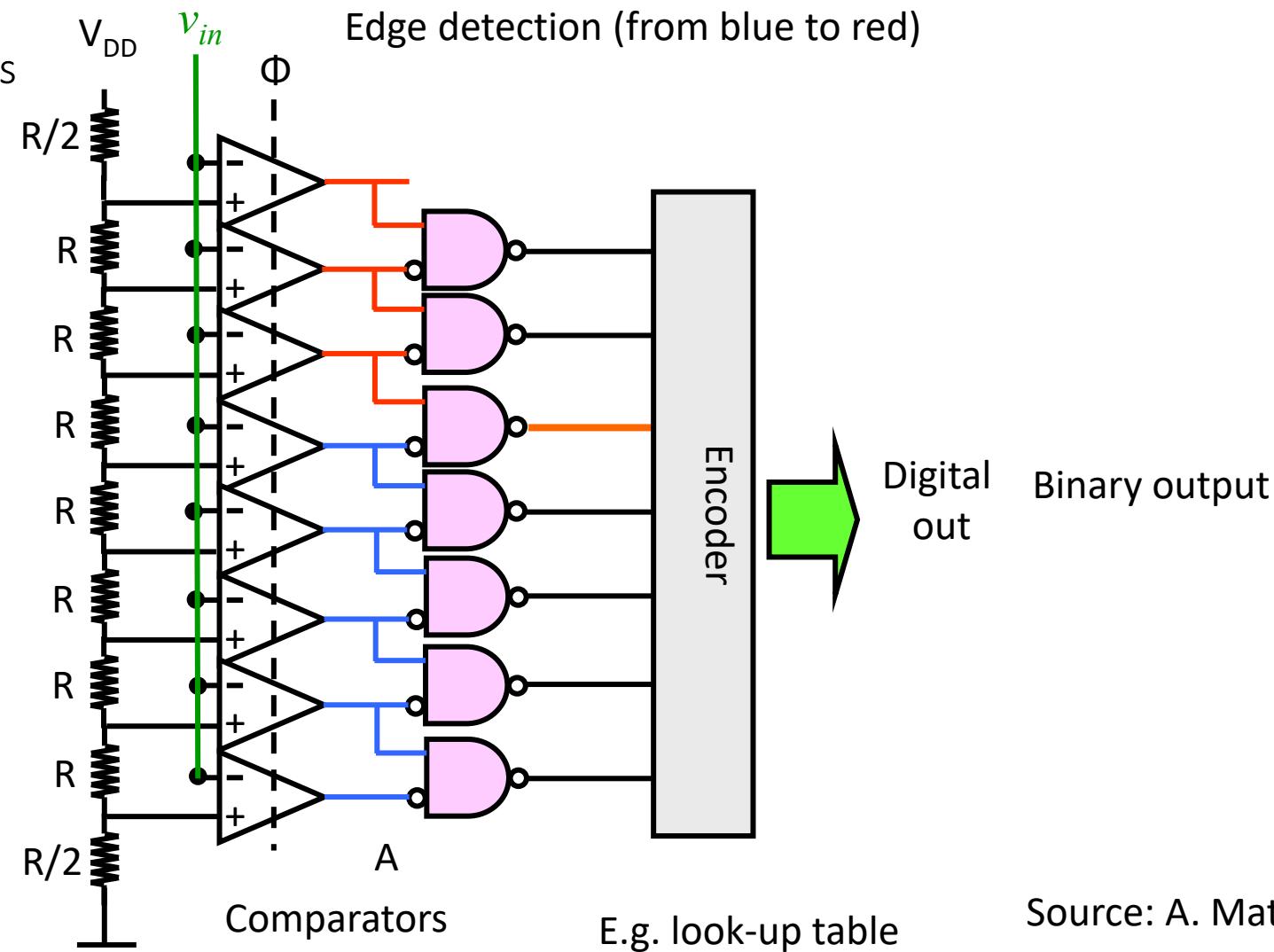
Source: A. Matzusawa

## 11.2.2 Flash (Direct Conversion) ADC

- Fundamental Components for N bit Flash (direct conversion) ADC:
  - $2^N$  comparators
  - $2^{N-1}$  Resistors
  - Control Logic

### Features:

- Low resolution (<8 bits)
- High power
- Ultra-high speed
- Large input capacitance



Source: A. Matzusawa

## 11.2.2 Flash (Direct Conversion) ADC

---

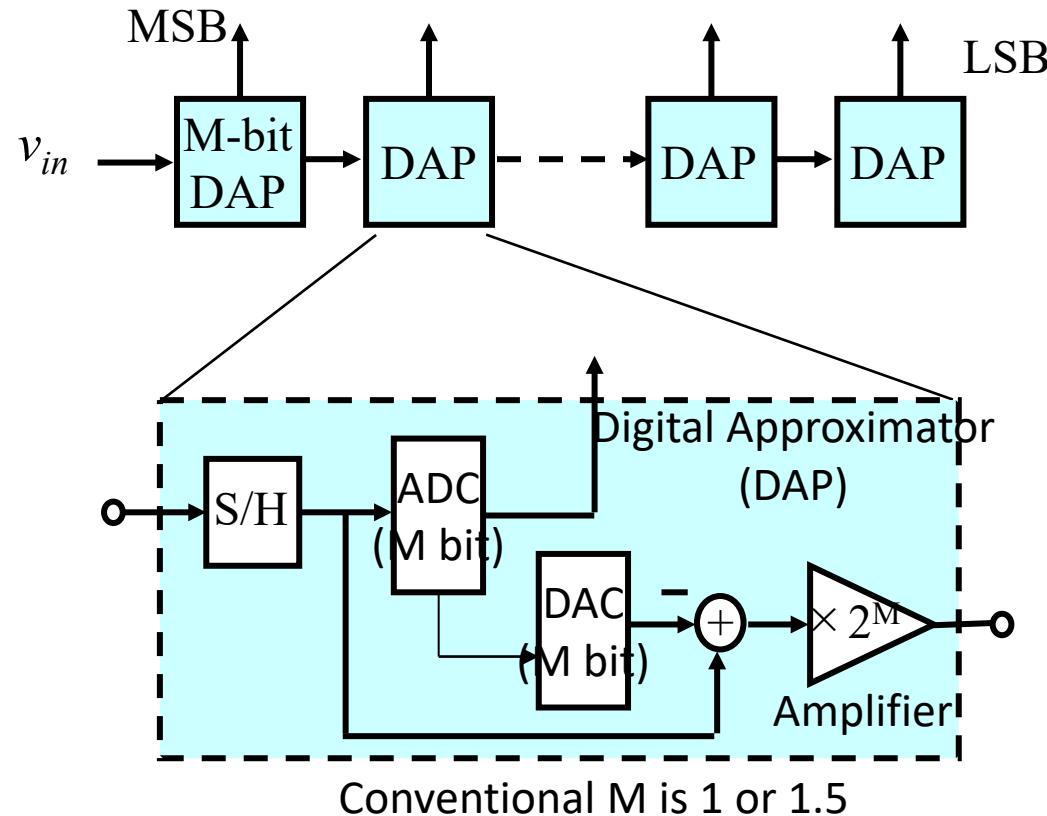
### Advantages

- Very fast (fastest)
- Very simple operational theory
- Speed is only limited by gate and comparator propagation delay

### Disadvantages

- Expensive
- Prone to produce glitches in the output
- Each additional bit of resolution requires twice the comparators

## 11.2.2 Pipelined ADC



- Each amplification stage reduces the input referred noise
- Stages can be sized accordingly

Features:

- High resolution (<20 bits)
- Low power
- Moderate speed
- Appropriate for column-parallel mode

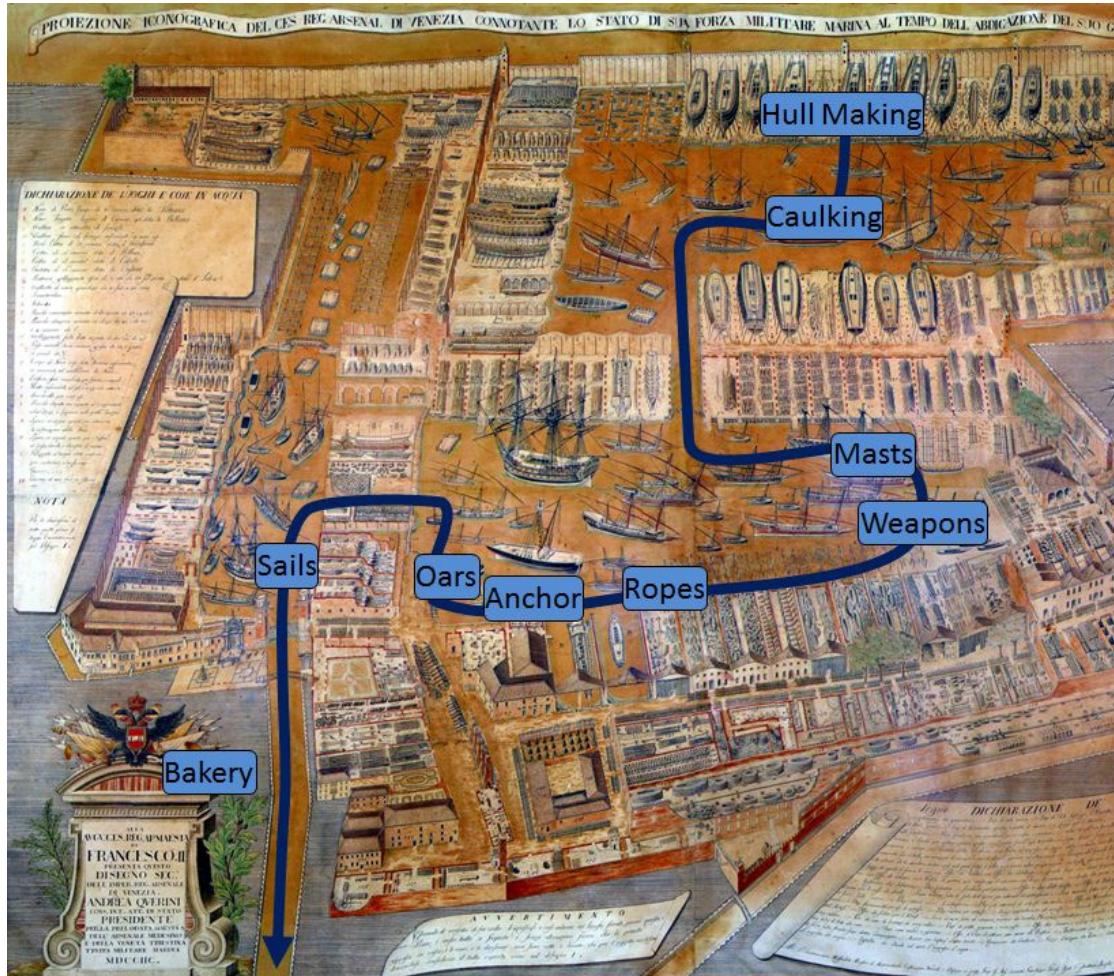
Refined version of successive approx. ADC, which has “only” a single comparator and DAC

Advantage: works in a pipeline fashion – don’t need to wait until a conversion finishes to start another one!

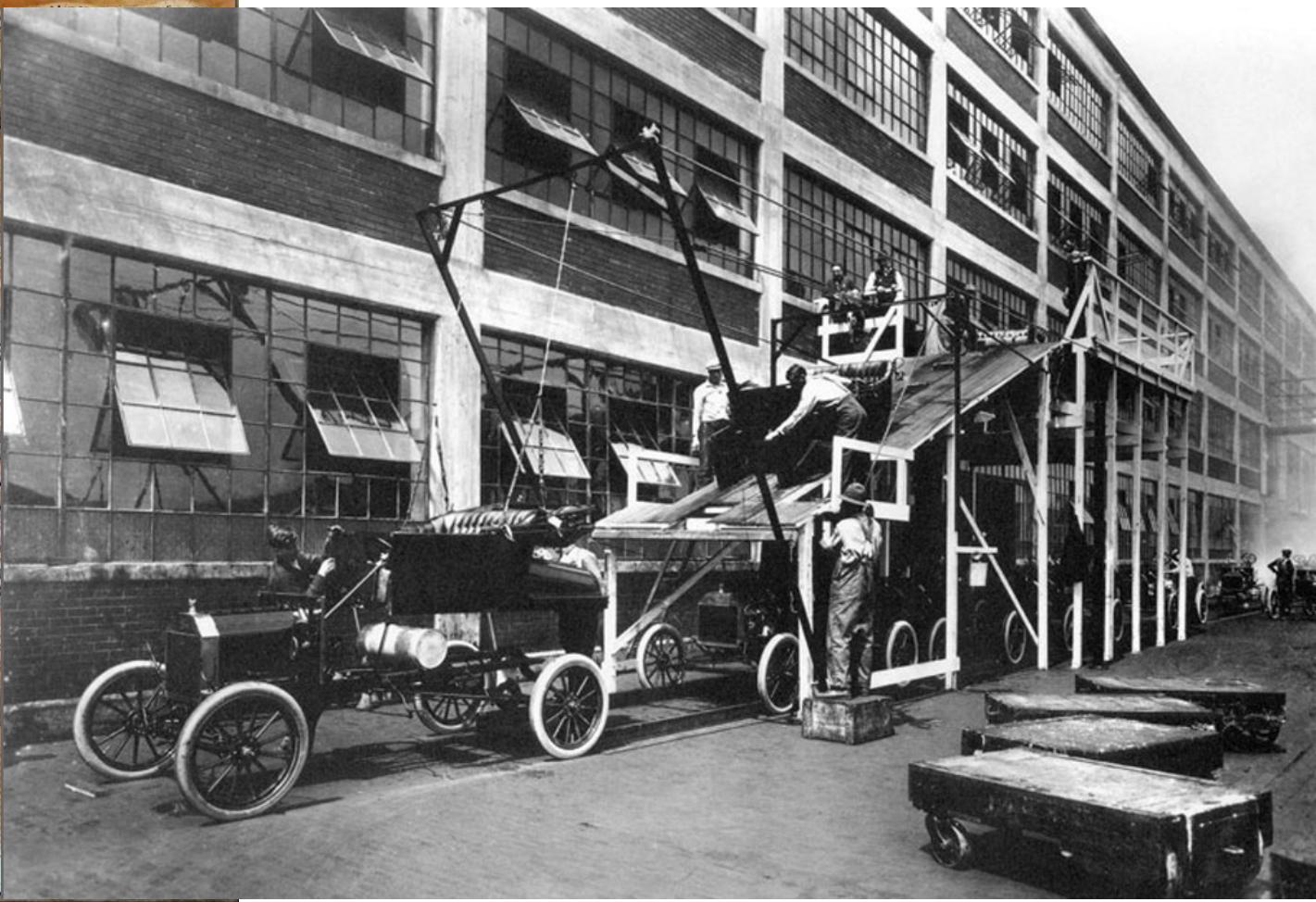
Source: A. Matzusawa

## 11.2.2 Assembly Line/Pipeline

Arsenal of Venice Material Flow Overview (1797)



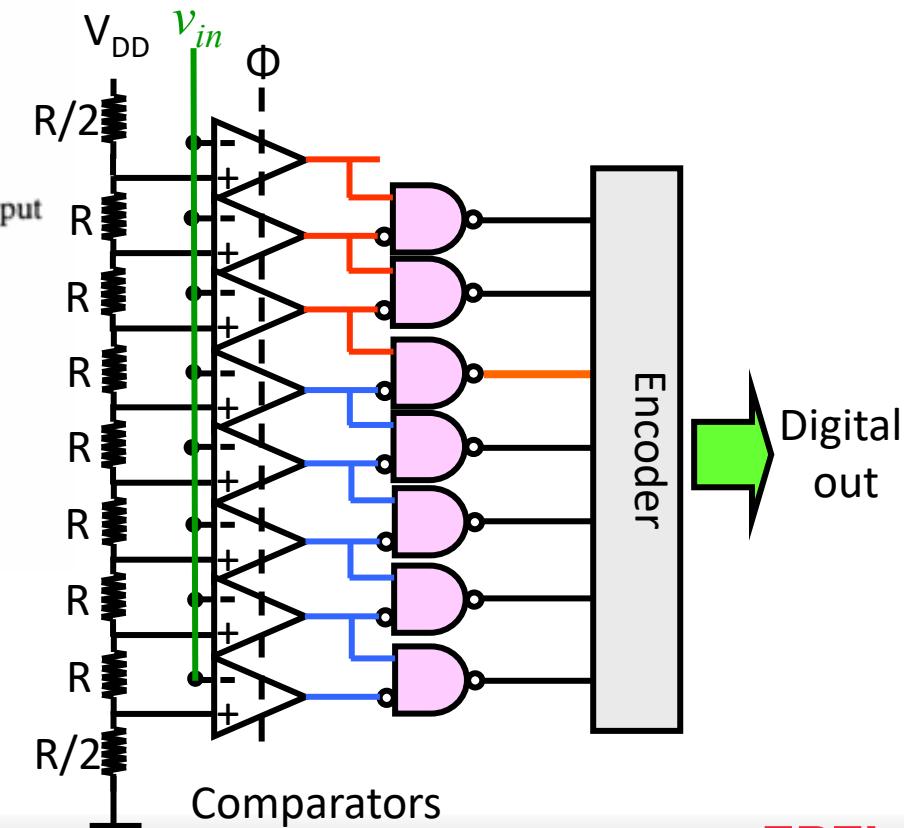
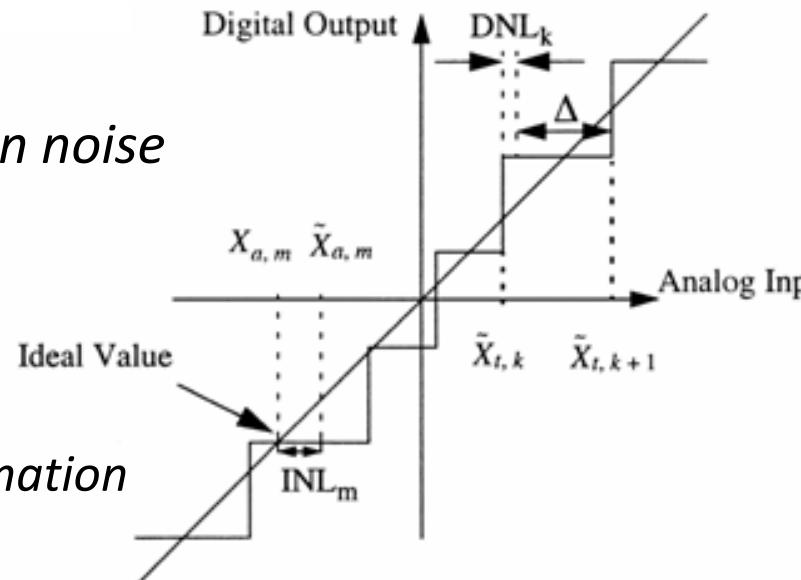
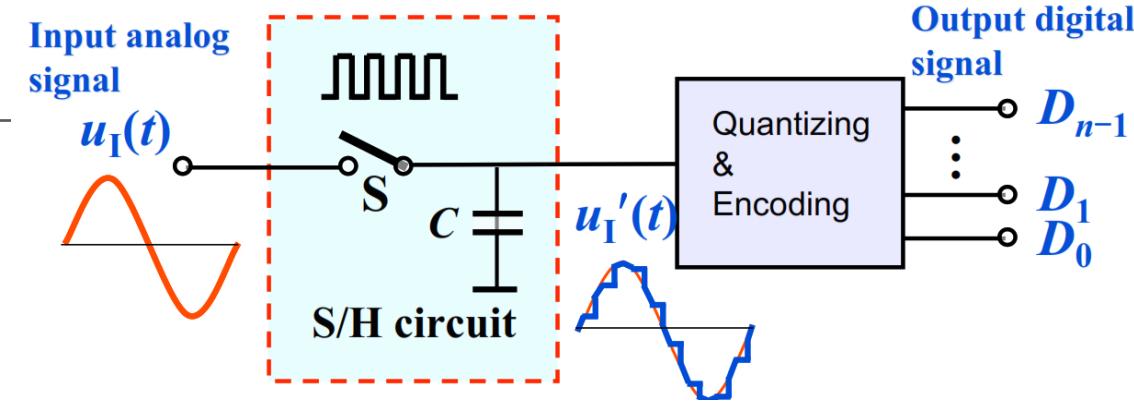
Henry Ford's Model T assembly line (1913)



<https://www.allaboutlean.com/material-flow-arsenal-of-venice/arsenal-of-venice-material-flow-overview/> <https://www.wwno.org/post/henry-fords-assembly-line-turns-100>

# Take-home Messages/W11-2

- Sampling of electrical signals
- Analog-to-Digital converters:
  - Basics
  - INL, DNL, Quantization noise
  - ADC architectures
    - Integrating
    - Successive-approximation
    - Flash
    - Pipelined



# Outline

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10.1 Charges, Currents, and Voltages

10.2 Noise Background

10.3 Noise Sources

11.1 Noise Reduction, Averaging Techniques

11.2 Electric Signals, Analog-to-Digital Conversion

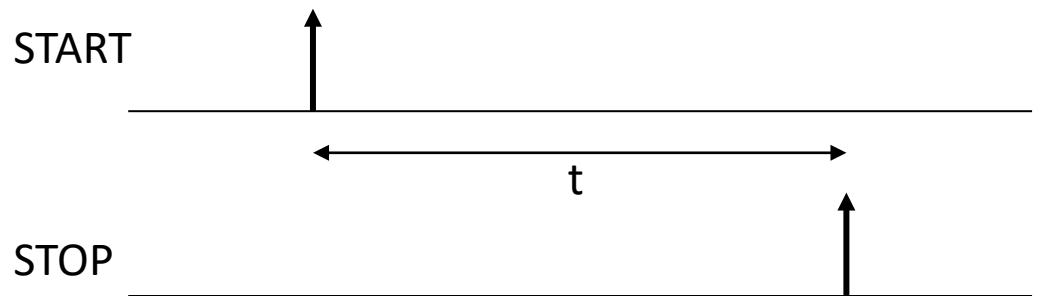
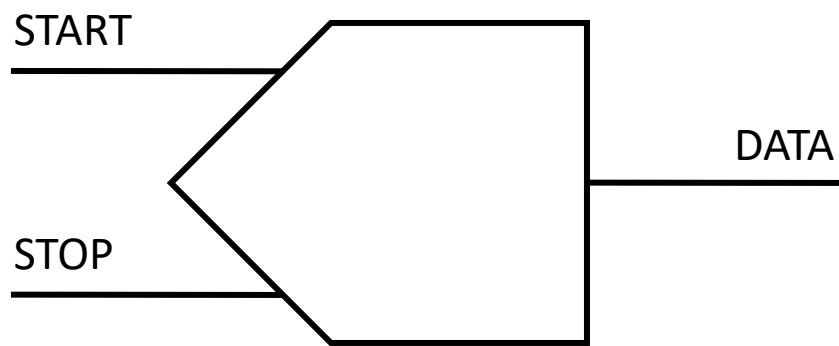
11.3 Timing – Time-to-Digital Conversion

12.1 Electrical Metrology Tools

## 11.3 Time to Digital Converter (TDC)

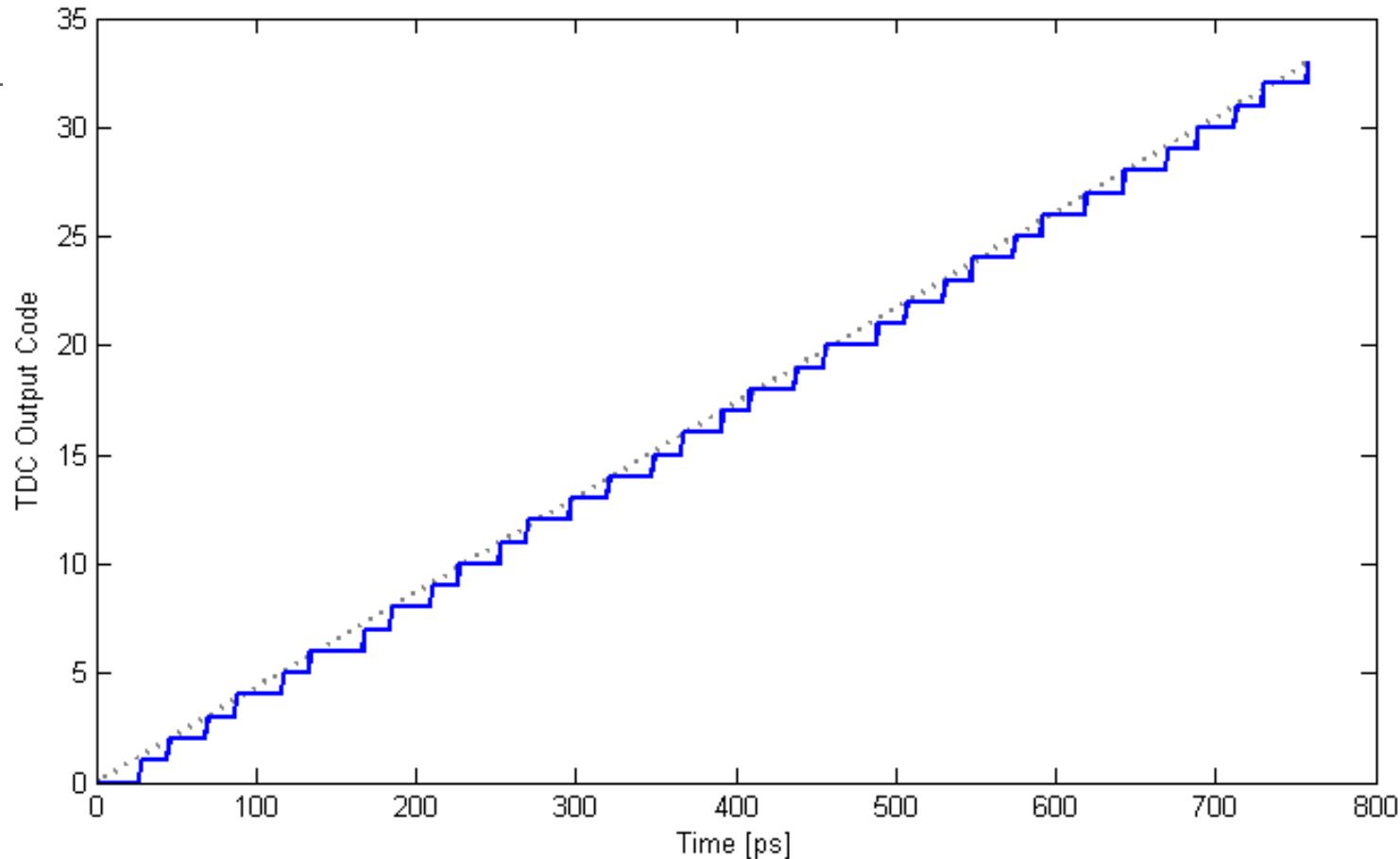
- TDCs have been used for more than 20 years in the field of particle and high-energy physics, where precise time-interval measurement is required.
- Time-to-Digital Converters (TDCs) are suitable for use in most time measurement applications.
- These TDCs measure time intervals from zero to the millisecond range at a resolution of better than 10ps.  

- These products are suitable for use in industrial, medical, automotive and scientific systems and equipment.



## 11.3 TDC – Nonidealities

- Signals are non-Dirac
  - Non-zero rise time
  - Non-zero width
- START-STOP sequence is not regular
- Signals (e.g. clocks) have jitter in
  - Time
  - Amplitude
- Temperature, Supply voltage, process variations -> PVT variations (process, voltage, temperature) -> process corners



# 11.3 TDC – Real Case

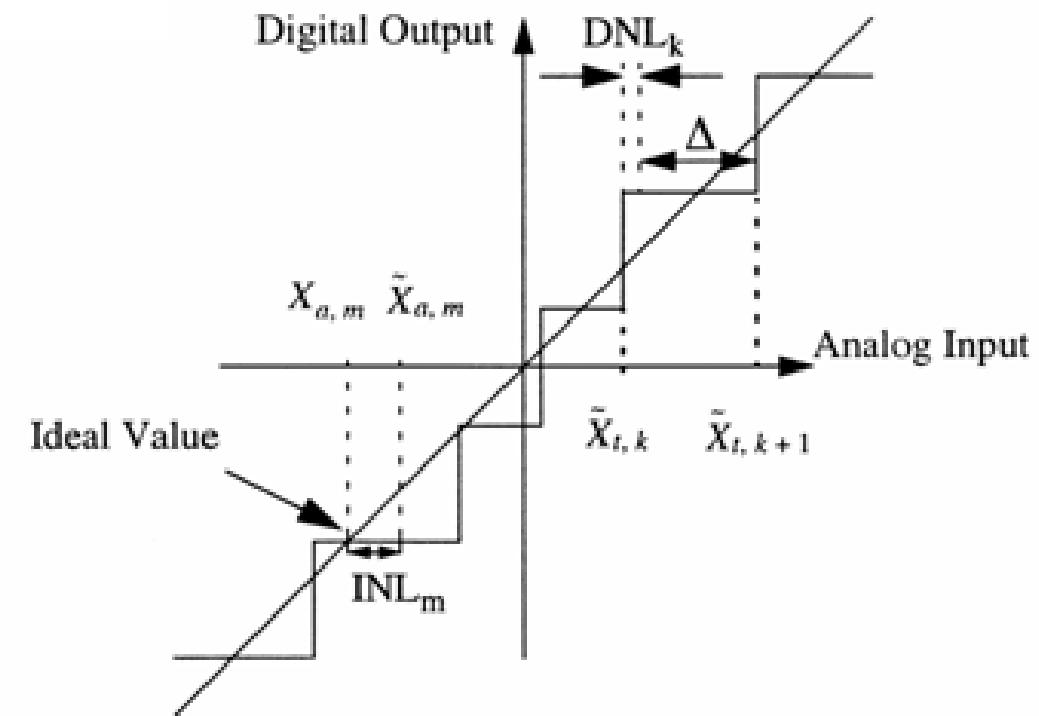
- Non-idealities

- Differential non-linearity (DNL)
- Integral non-linearity (INL)

$$DNL_j \equiv \frac{Width_{ACTUAL,j} - Width_{IDEAL}}{Width_{IDEAL}}$$

$$INL_j = \sum_{k=0}^{k=j} DNL_k$$

$$DNL_j = INL_{j+1} - INL_j$$



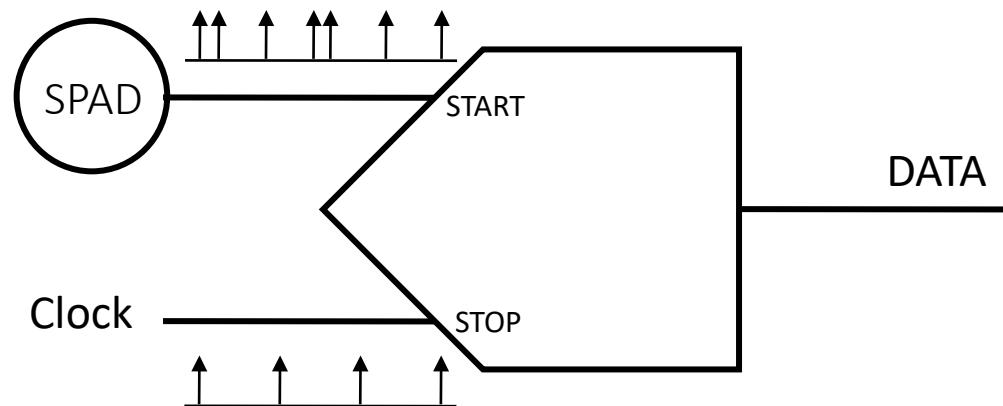
Width on x-axis: time bin width.

# 11.3 TDC – Metrology: Optical Tests

A) (Code) Density test: free running SPAD (e.g. natural light source)\*

B) Single-shot experiment (e.g. repetitive pulsed laser illumination):

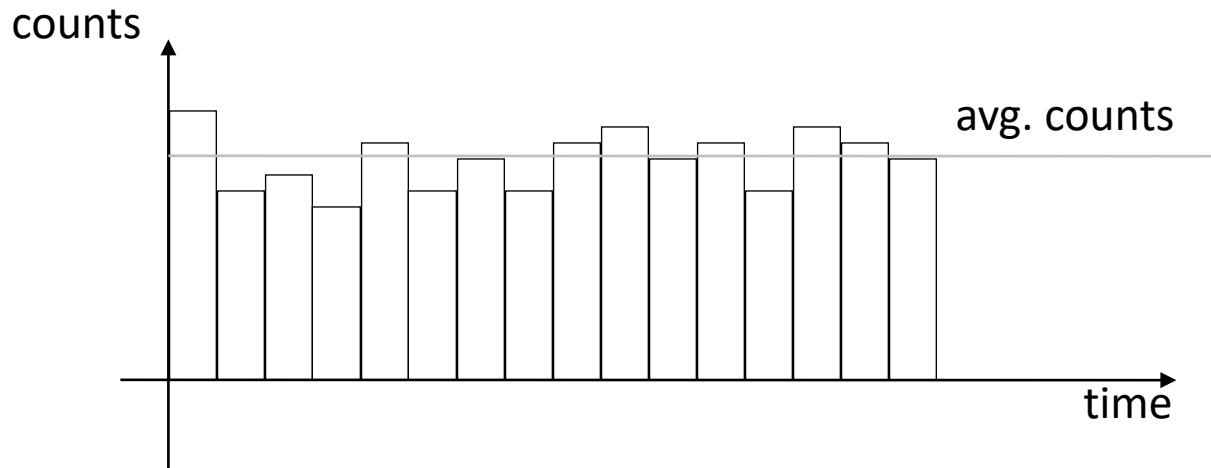
- Histogram  $\Delta t_i, i=[1\dots N]$  (Time-correlated single-photon counting – TCSPC)



\*could also be done electrically

# 11.3 TDC – Metrology: (Code) Density Test

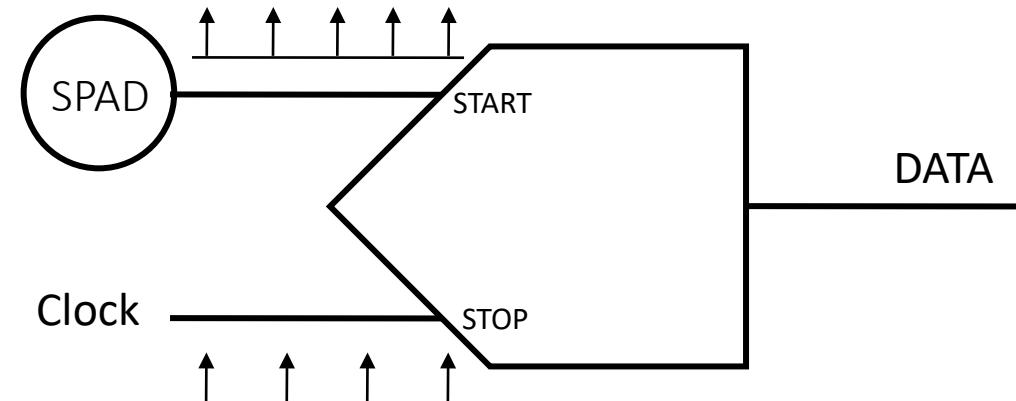
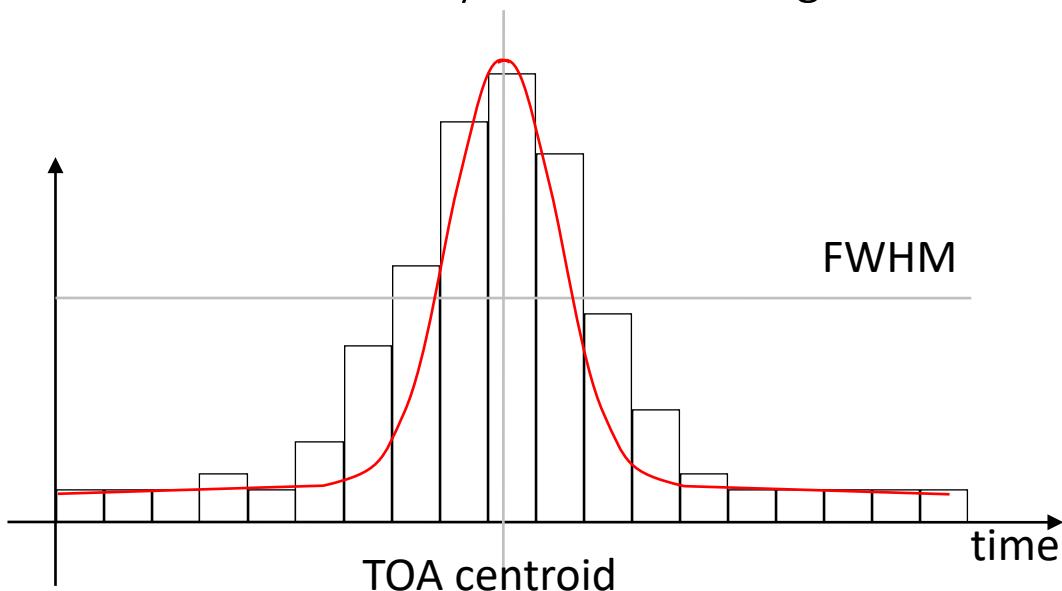
- Poisson-distributed uniform START generator (e.g. by using a free running SPAD and a natural light source – no laser)
- Measure statistics of TDC measurements per bin
- Normalize to average counts  $\rightarrow$  differences are DNL points



# 11.3 TDC – Metrology: Single Shot Precision

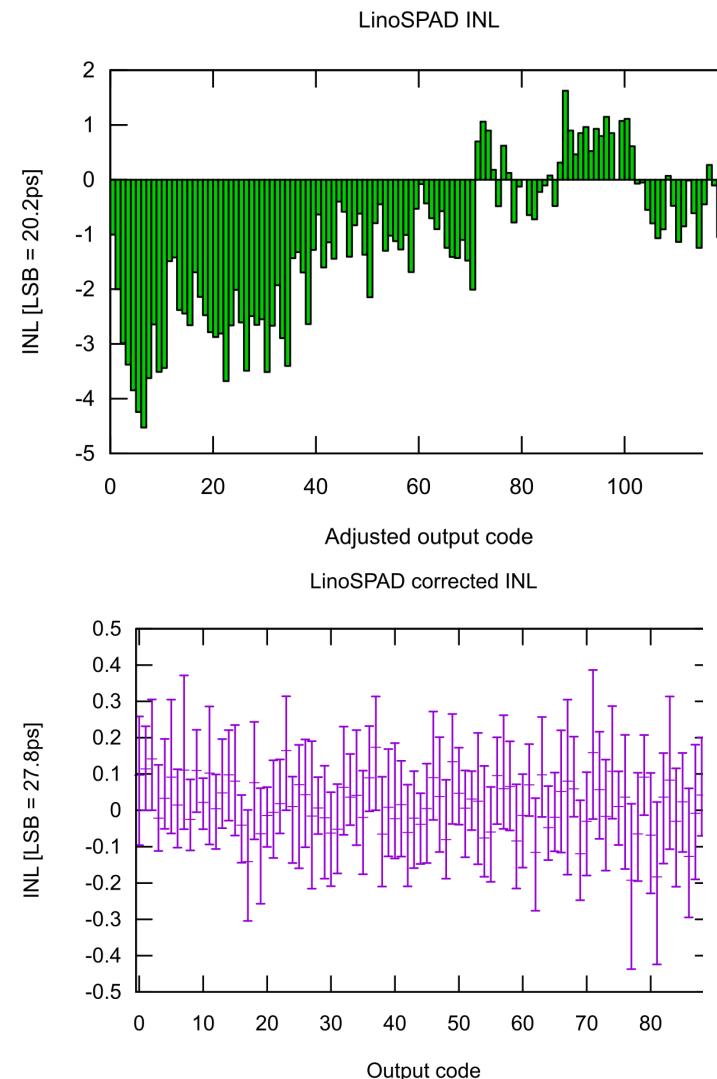
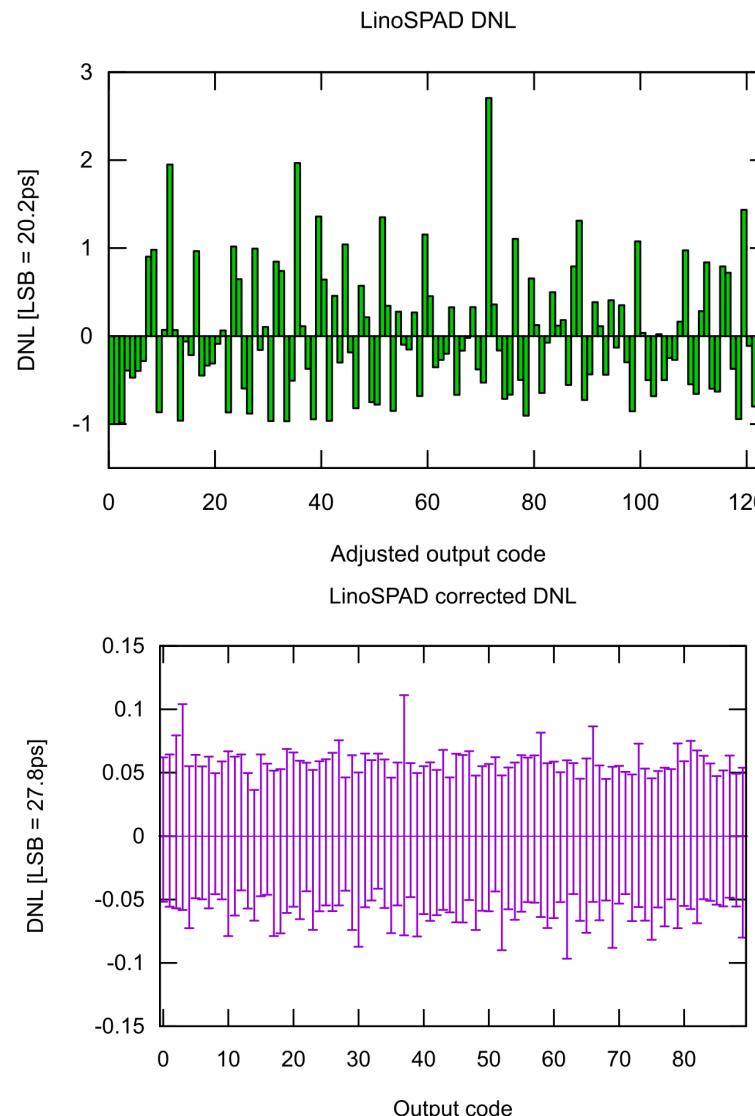
Q

- Repeat measurement of single time-of-arrival (e.g. with [pulsed laser](#) at fixed repetition frequency) and construct histogram
- Derive statistics by Gaussian fitting and calculation of FWHM or  $\sigma$  or  $3\sigma$ .



The resulting (Gaussian) timing distribution contains all measurement uncertainties, combined quadratically if independent

# 11.3 TDC – DNL vs INL and Accuracy



Calibration of a  
Time-to-Digital  
converter  
S. Burri, EPFL, MDPI  
Instruments, 2018



High Precision, High Accuracy



Low Precision, High Accuracy



High Precision, Low Accuracy



Low Precision, Low Accuracy

## 11.3 TDC – Architectures

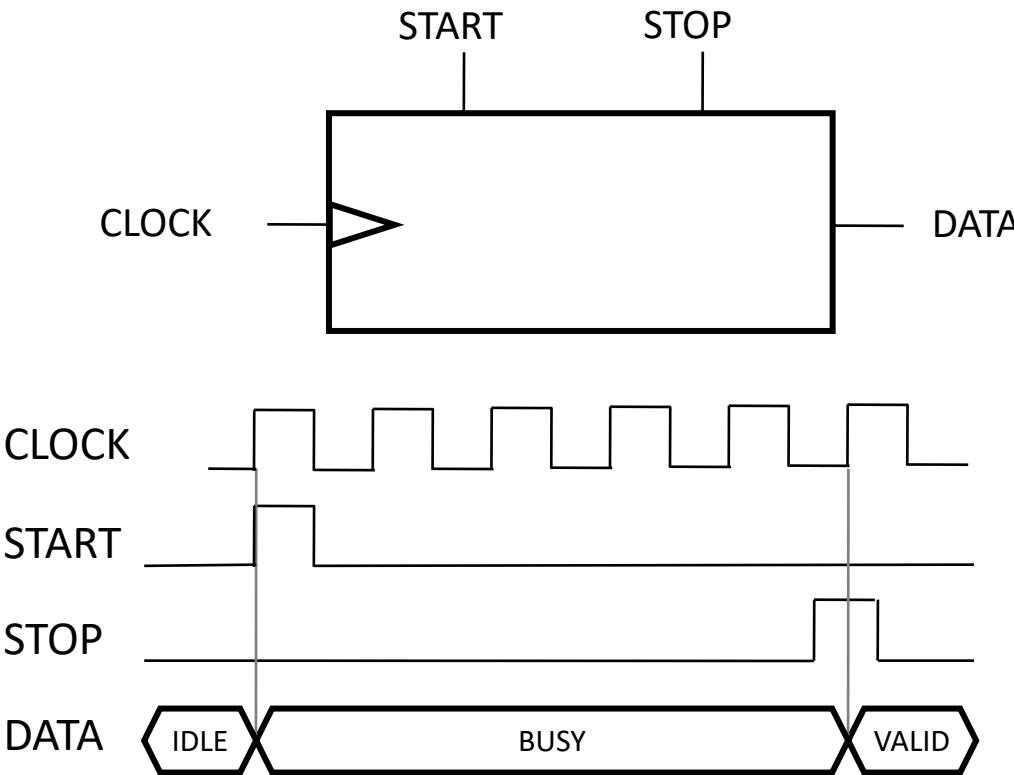
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- Counter – Register
- Delay Chain
- Phase Interpolator
- Vernier Lines
- Pulse Shrinking
- Ring Oscillators

## 11.3.1 TDC: Counter - Register

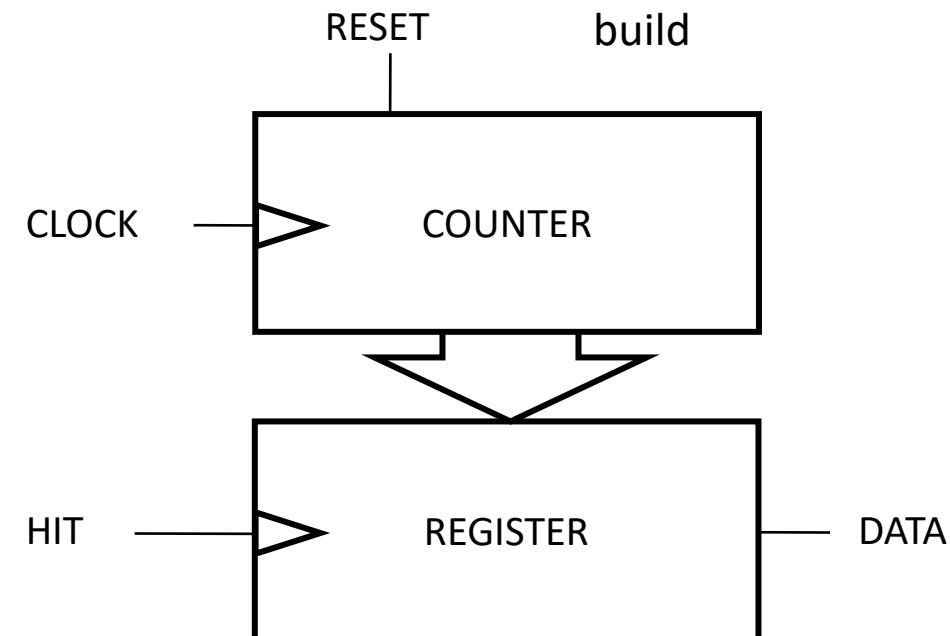
- Resolution:  $\tau = 1/f_{\text{clock}}$  
- Conversion rate = 1/latency

Latency = time necessary to do one full conversion.  
Simply count the # of clock cycles.



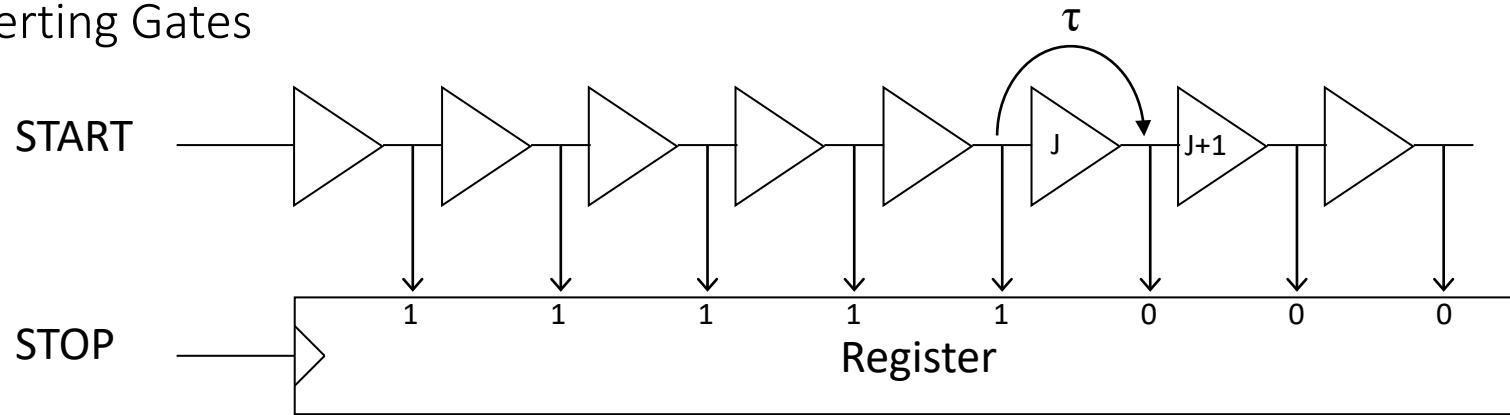
### Advantages

- Fast counter can be shared among many HIT lines
- Fast registers easier to build



## 11.3.2 TDC: Delay Chain

- Non-Inverting Gates

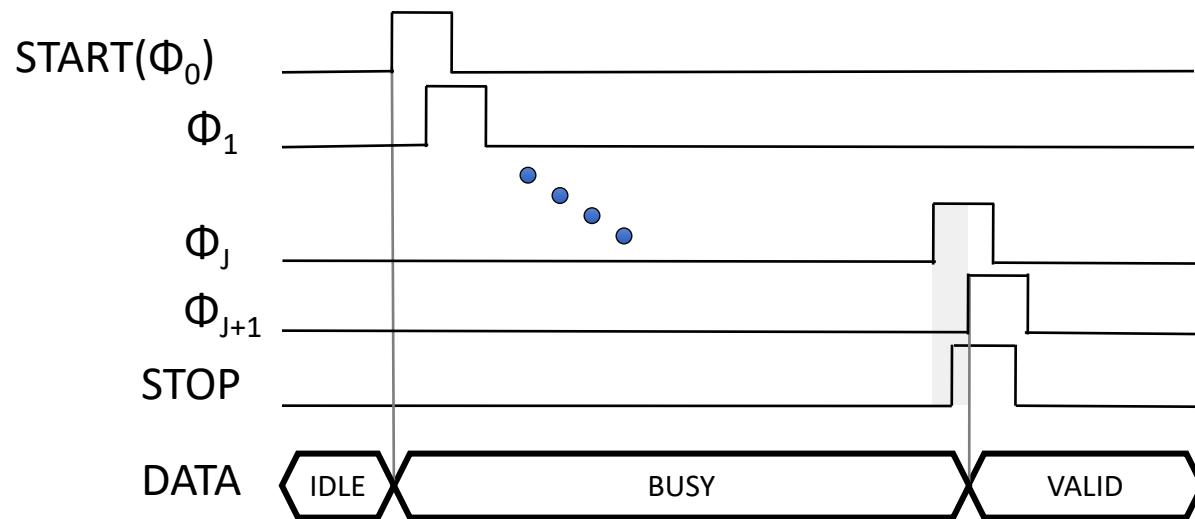


START = signal, STOP = clock.

Signal propagates and clock freezes the registers.

Tau = time for one gate transition, can be in the 10's of ps range.

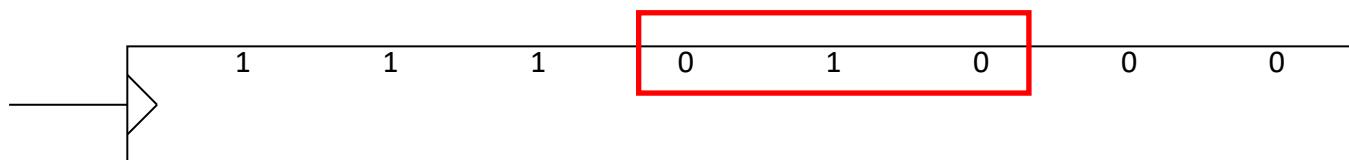
Gate = simple buffers.



## 11.3.2 TDC: Delay Chain

---

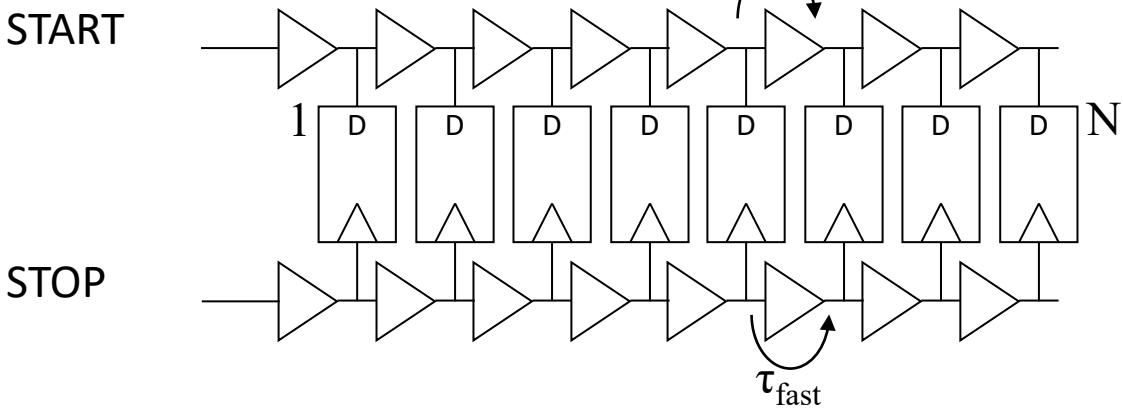
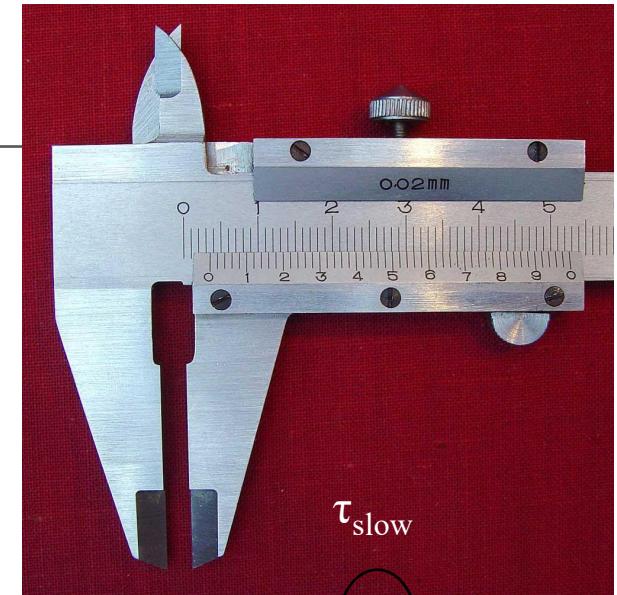
- Resolution:  $\tau = \text{delay element}$
- Conversion rate = 1/latency
- Latency =  $N \times \tau$
- Need a thermometer decoder:  $N \rightarrow \log_2(N)$
- Issues: metastability, bubbles



### 11.3.3 TDC: Vernier Lines

- Resolution:  $\tau = \tau_{\text{slow}} - \tau_{\text{fast}}$  (does not depend on a gate delay!),  
 $T = n(\tau_{\text{slow}} - \tau_{\text{fast}})$
- Conversion rate = 1/latency
- Latency =  $N \times \tau_{\text{slow}}$
- Need a thermometer decoder:  $N \rightarrow \log_2(N)$
- Each stage consists of two buffers and one flip-flop
- Issues: metastability, matching

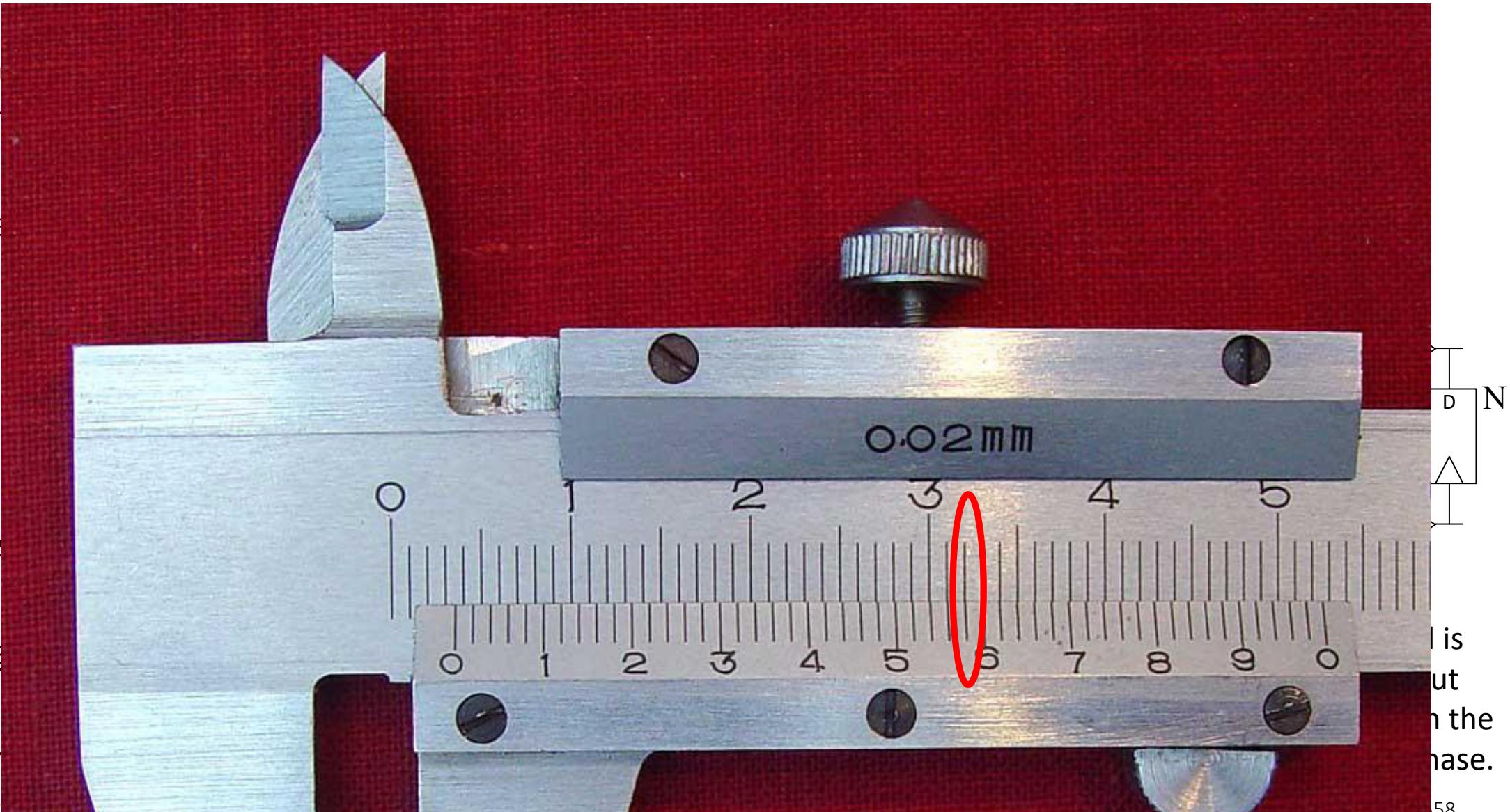
Pierre Vernier, 1631



Two delay lines, a fast and a slow one. The START signal is injected in the slow one. The STOP signal occurs later but propagates faster and catches up at a certain point with the slow one -> detection of the point where both are in phase.

### 11.3.3 TDC: Vernier Lines

- Resolution:  $T = n \cdot \Delta x$
- Conversion
- Latency
- Need to calibrate
- Each step is  $\Delta x$
- Issues



Pierre Vernier, 1635

E. Charbon, "Image Series"

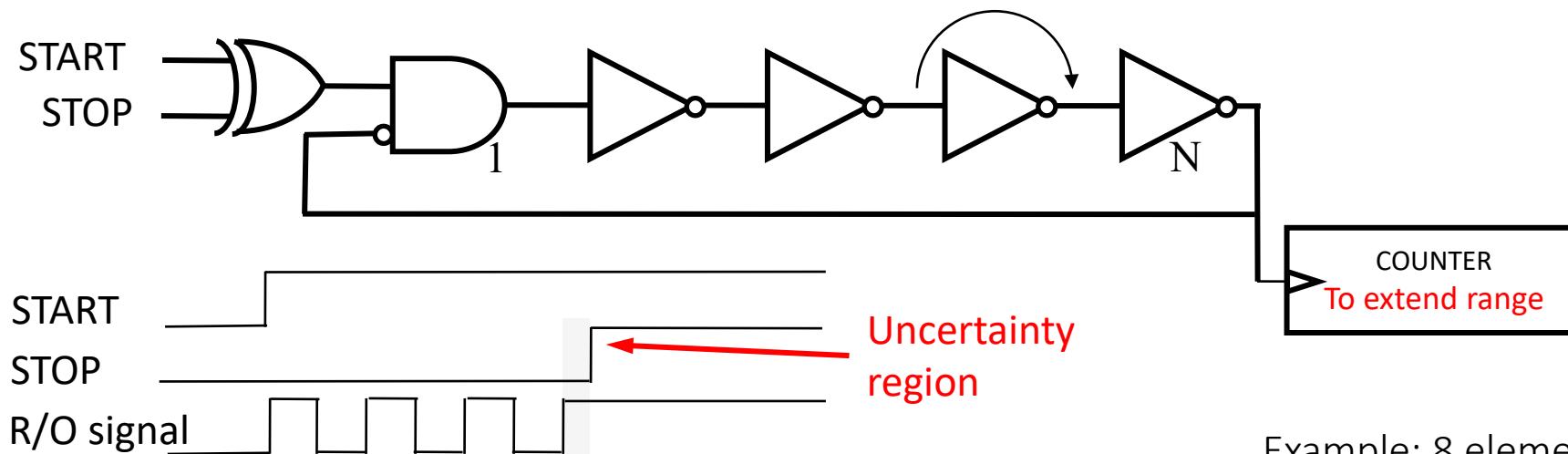
58

## 11.3.4 TDC: Ring Oscillator

- Resolution:  $\tau = \text{delay element}$
- Conversion rate = 1/latency
- Latency =  $N \times \tau$
- Need a thermometer decoder:  $N \rightarrow \log_2(N)$
- Issues: metastability, matching, asymmetric load

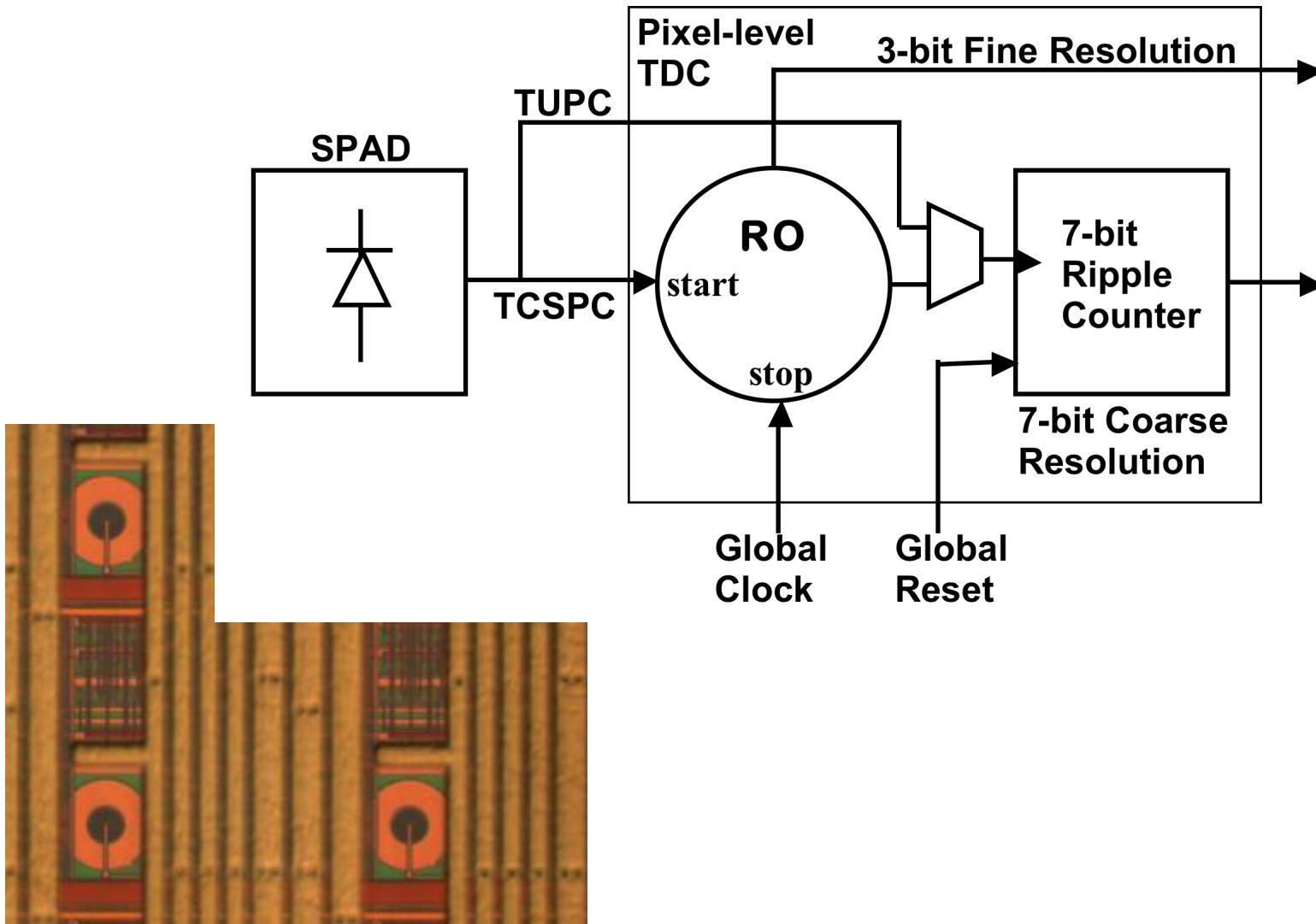
Main idea: have the signal recirculating instead of using a long linear chain. Circulates until the stop signal comes.

Each time it circulates, a counter is incremented -> can use much less delay elements.



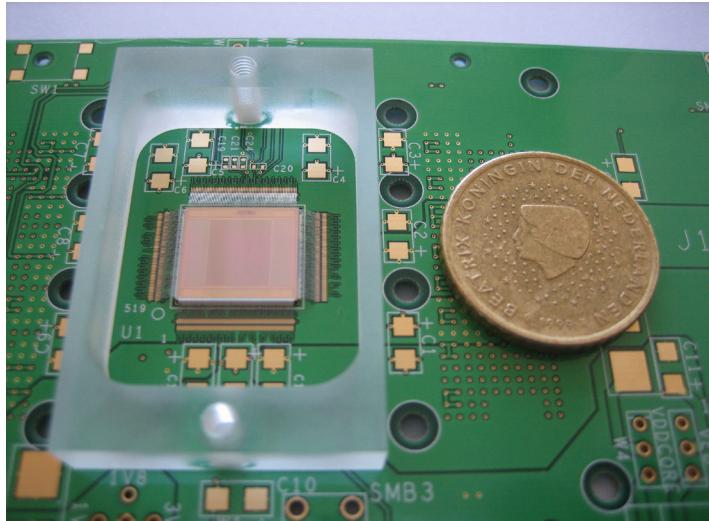
Example: 8 elements -> 3 bits

## 11.3.6 TDC: Example: MEGAFRAME Pixel



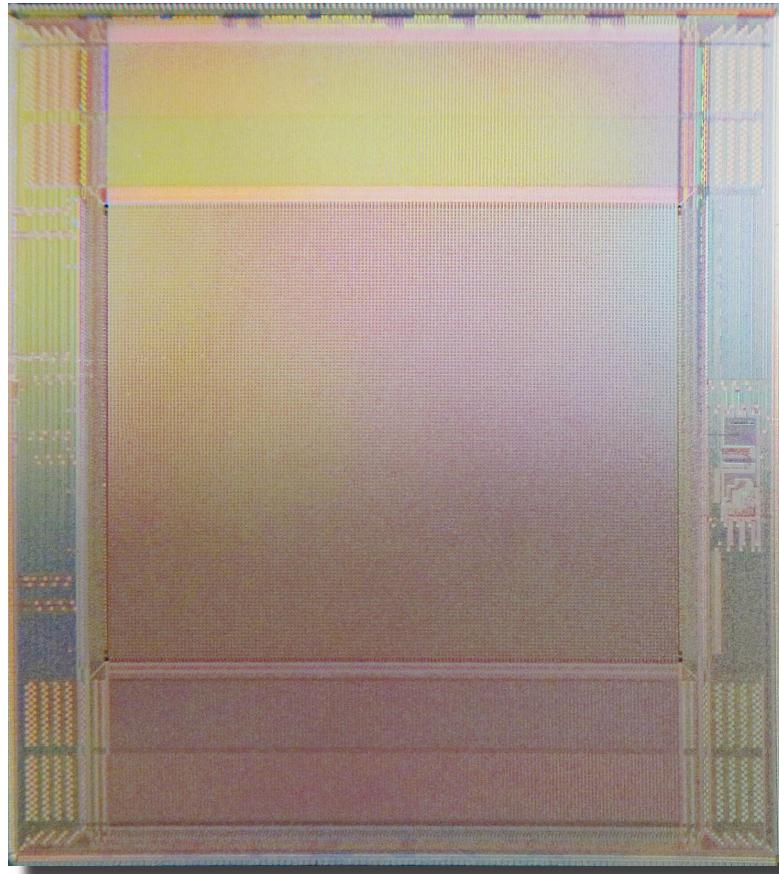
## 11.3.6 TDC: Example: MEGAFRAME Pixel

- Format: 160x128 pixels
- Timing resolution: 55ps
- Impulse resp. fun.: 140ps
- DCR (median): 50Hz
- R/O speed: 250kfps
- Size: 11.0 x 12.3 mm<sup>2</sup>

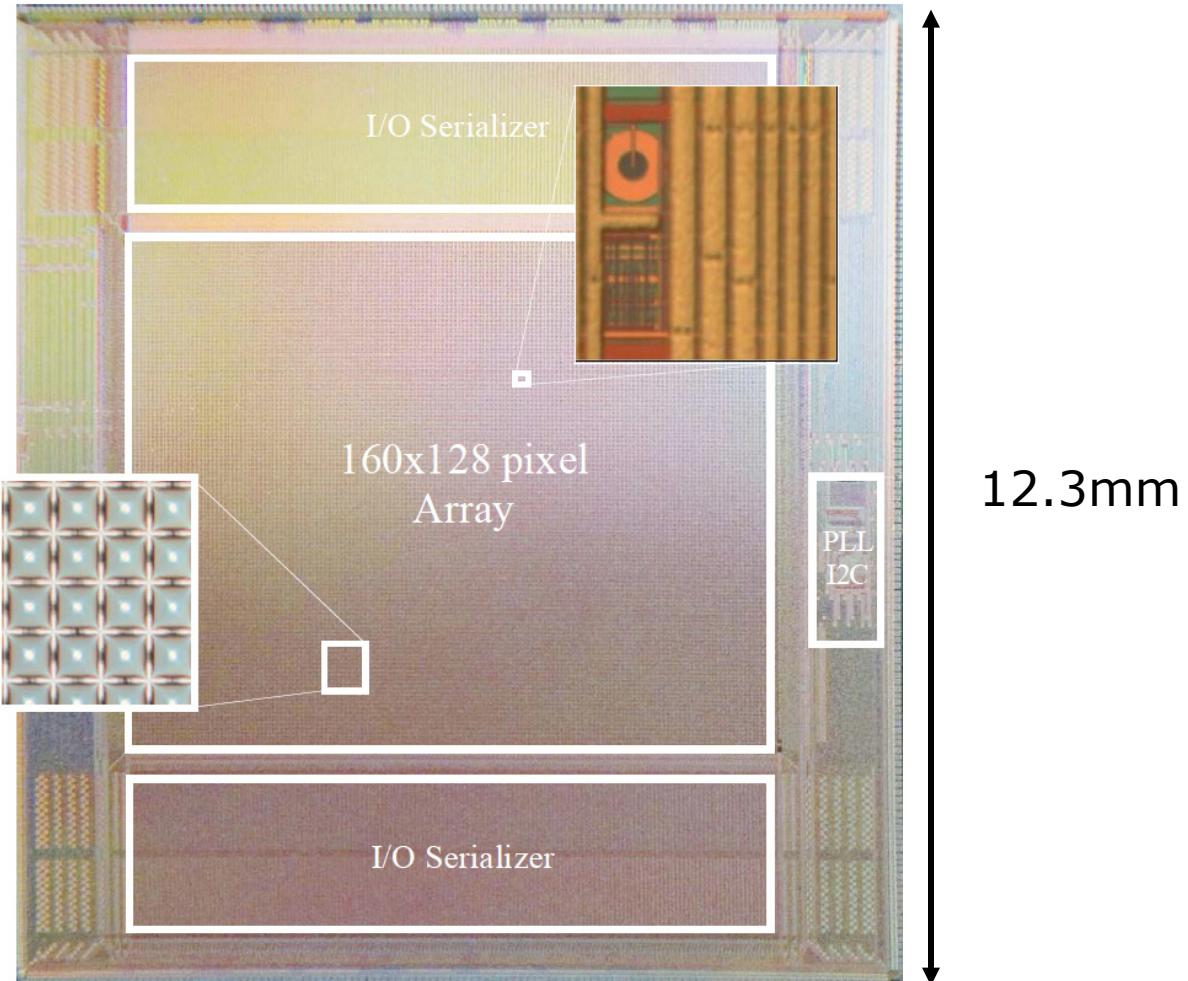


TDC

Ring oscillator (3 bits) + counter (7 bits) = 10 bits



## 11.3.6 TDC: Example: MEGAFRAME Pixel



C. Veerappan, J. Richardson, R. Walker, D.-U. Li, M. W. Fishburn, Y. Maruyama, D. Stoppa, F. Borghetti, M. Gersbach, R.K. Henderson, E. Charbon, *ISSCC2011*

## 11.3.8 TDC Summary: Basic Definitions

Bin size or resolution –  $\tau$  (sec)

- Minimum distance between time events that can be resolved [LSB]

Range (sec)

- Maximum time difference that can be measured

Conversion rate (MS/sec)

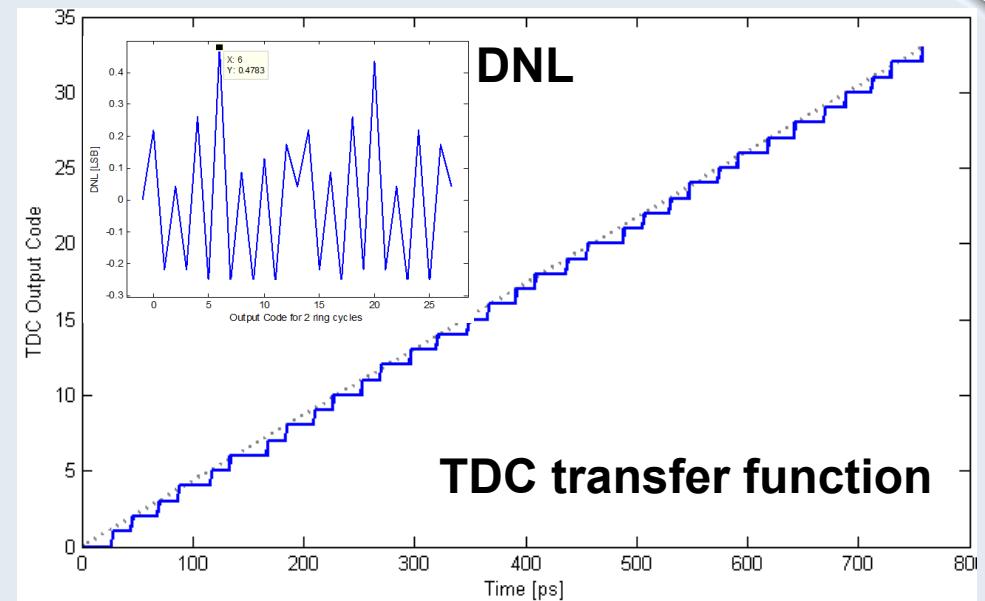
Latency (sec)

Non-linearities (LSB)

- Differential non-linearity (DNL)
- Integral non-linearity (INL)

Single-shot precision (sec)

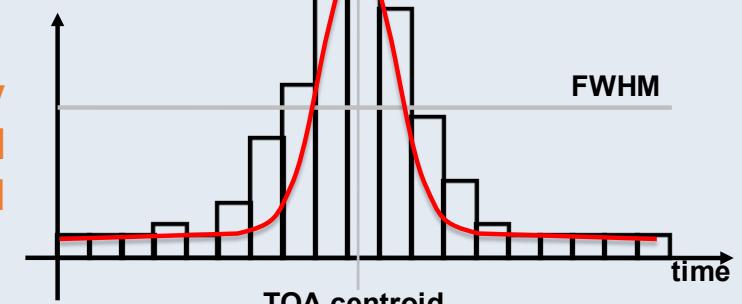
**TDC non-ideality**



**TDC transfer function**

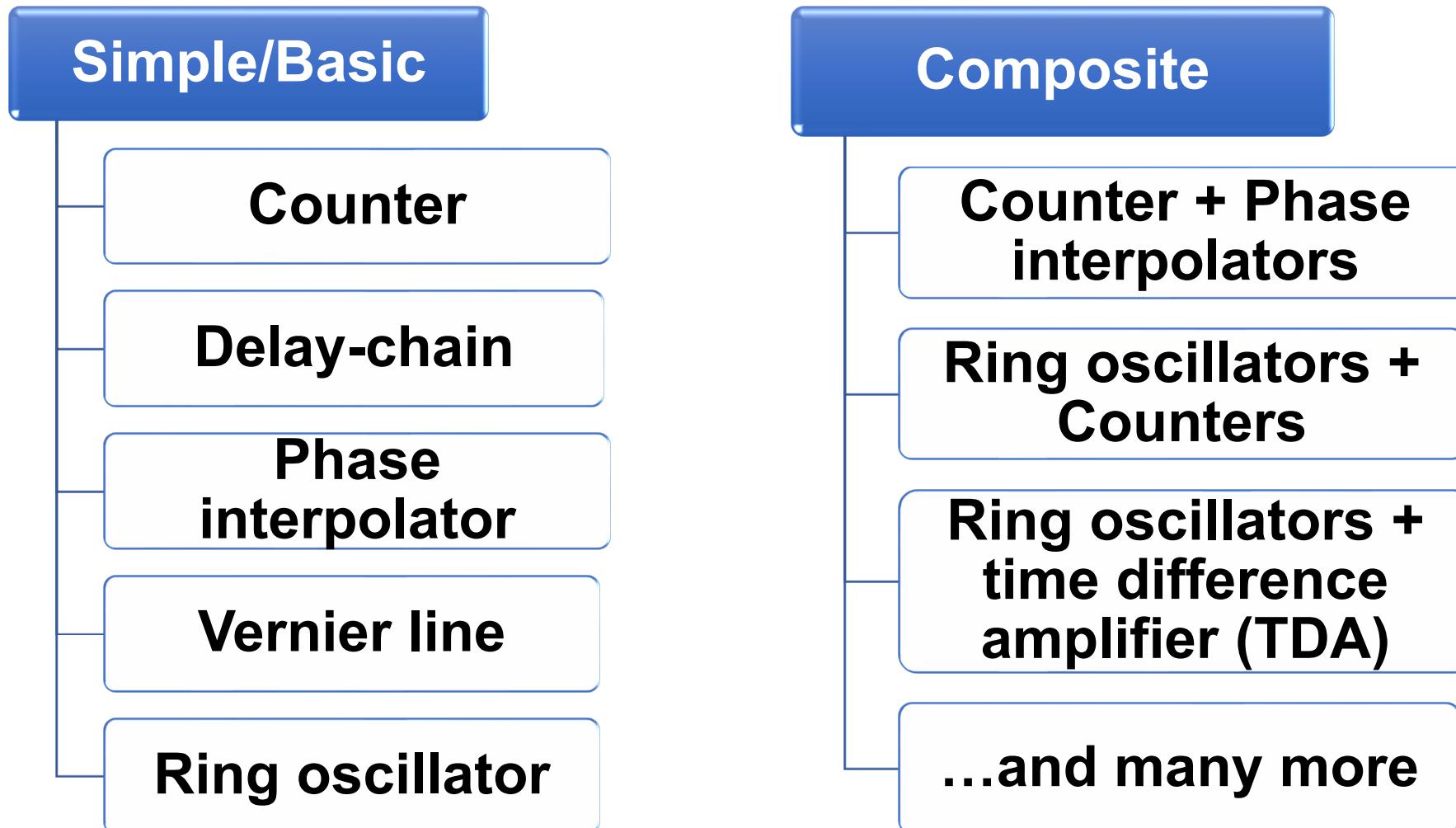
**SSA**

Derive statistics by Gaussian fitting and calculation of FWHM or  $\sigma$  or  $3\sigma$ .



**Histogram representation**

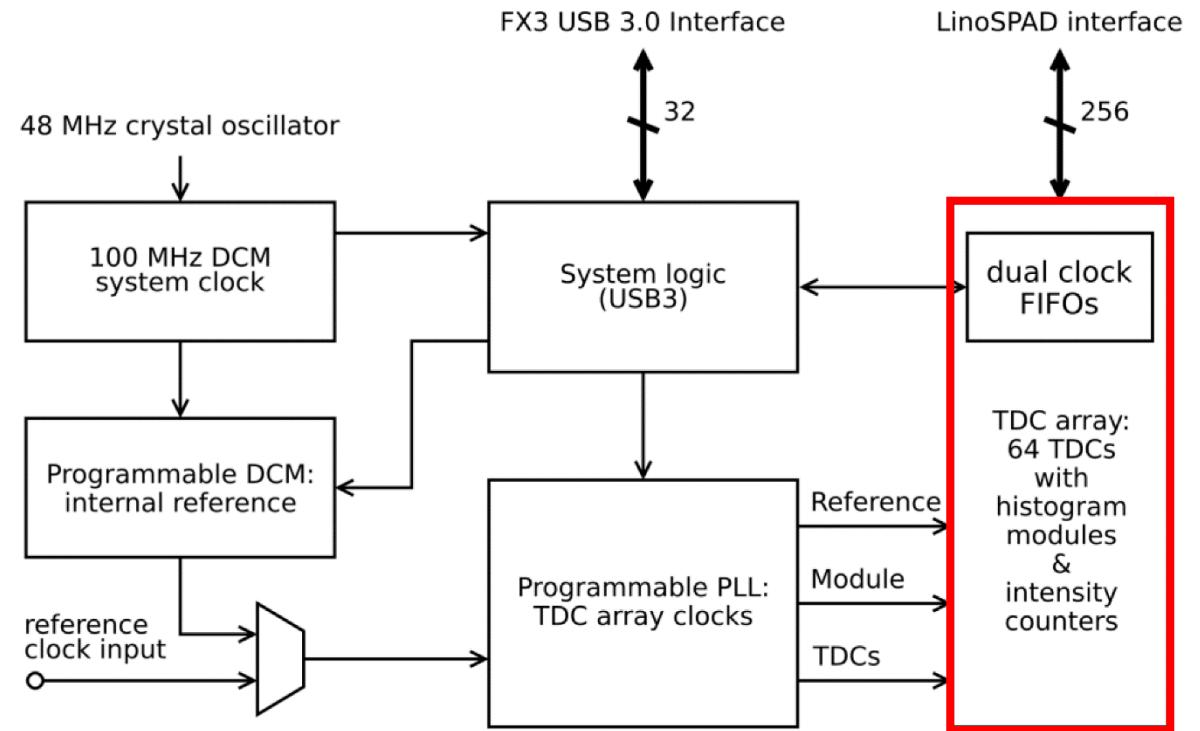
## 11.3.8 TDC Summary: Architectures



## 11.3.8 TDC implementations (on FPGAs)

### TDC implementation

- ✓ On ASICs
- ✓ On FPGAs



**FPGA TDC example- LinoSPAD camera**

[S. Burri et al., Sensors 2017]

## 11.3.9 TDC Application Example: Time-resolved Imaging

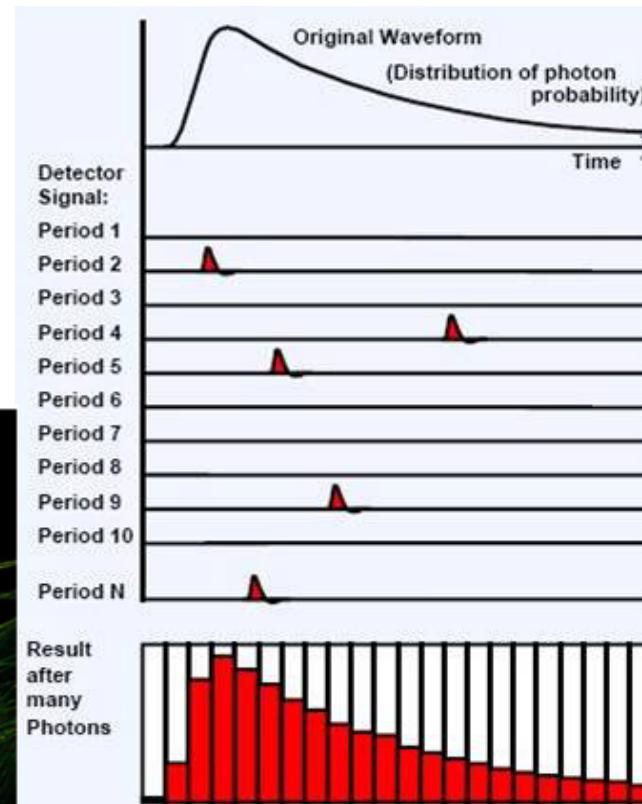
- Suppose you could timestamp or gate every photon you detect -> time-resolved detector
- Suppose an imager comprises a number of pixels with a time-resolved detector -> time-resolved imager or time-resolved image sensor

High Speed Binary Imaging

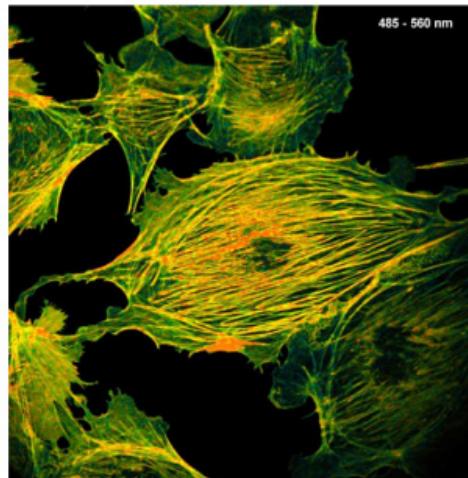


(a)

Time-Correlated Single Photon Counting



Nanosecond  
Lifetimes!



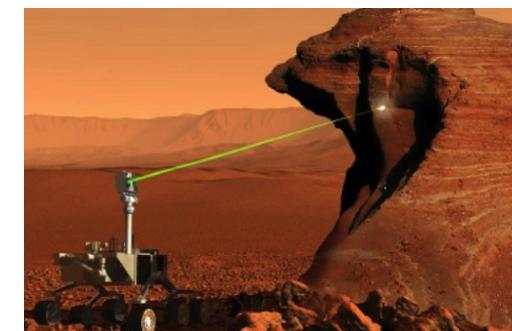
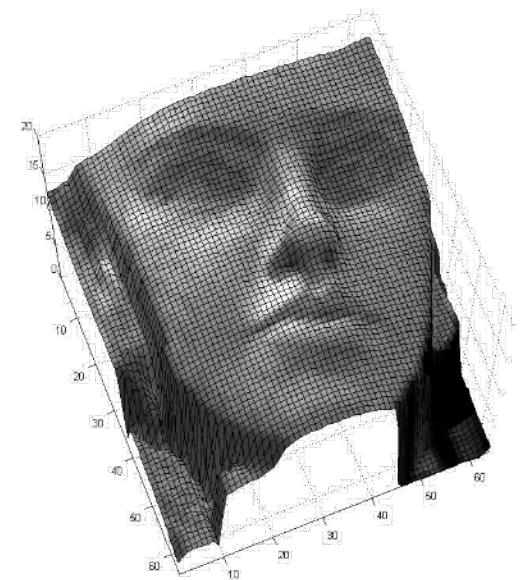
Light Detection and Ranging



cm/mm level precision!

## 11.3.9 TDC Application Example: Time-resolved Imaging

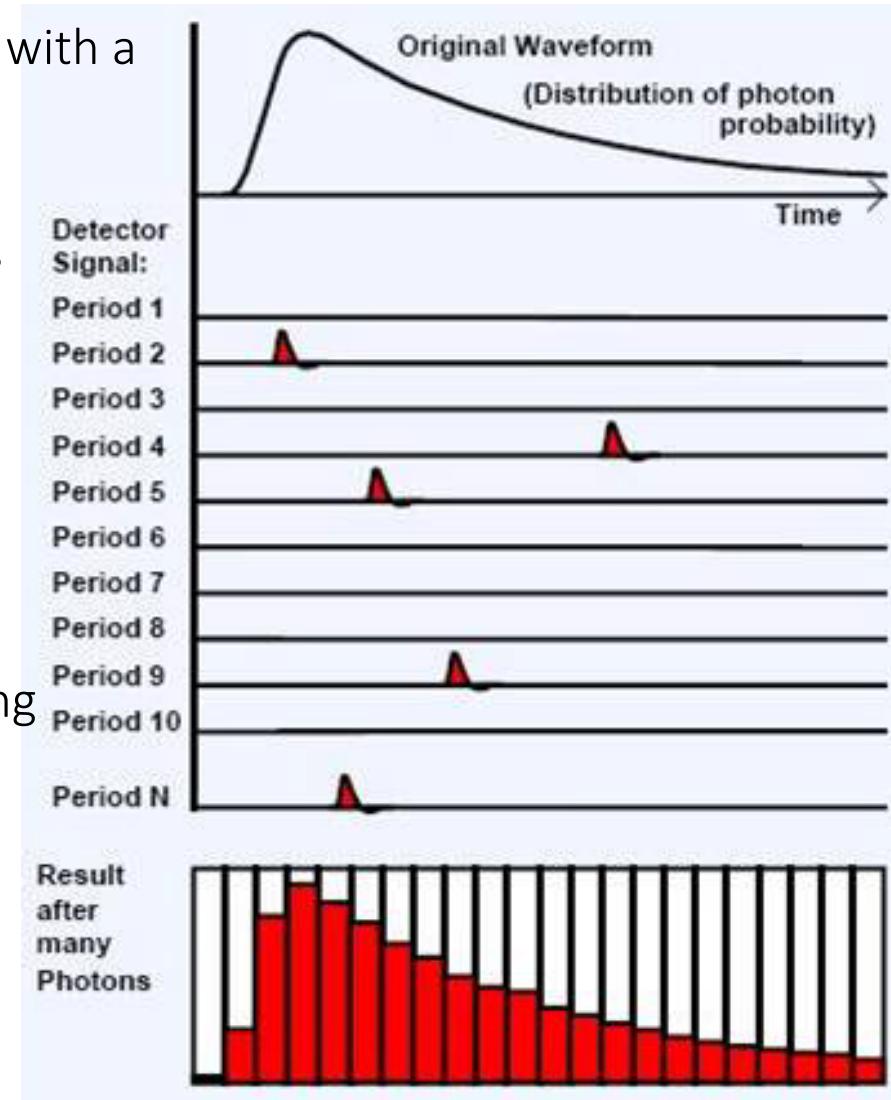
- **3D imaging**
  - Mechanism: time-of-flight (TOF) detection
- **Molecular imaging**
  - Mechanism: fluorescence lifetime imaging microscopy (FLIM)
- **Positron emission tomography**
  - Mechanism: time-coincidence of gamma rays originated from a positron-electron annihilation
- **Time-resolved Raman spectroscopy**
  - Mechanism: time-gating for fluorescence filtering
- Or simply, fast or strobe imaging for scientific applications



## 11.3.9 TDC Application Example: TCSPC

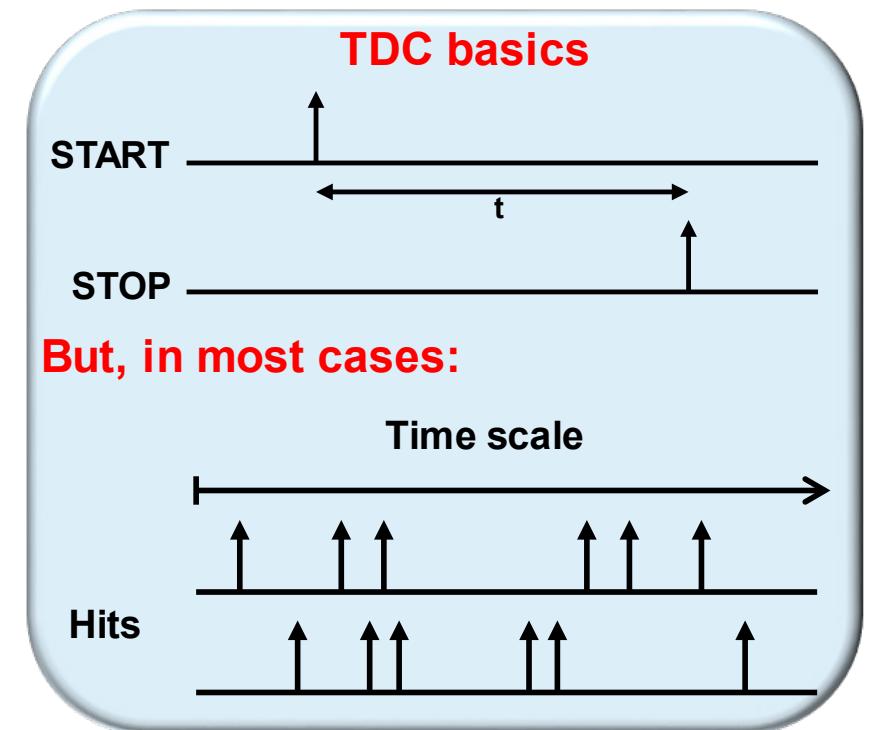
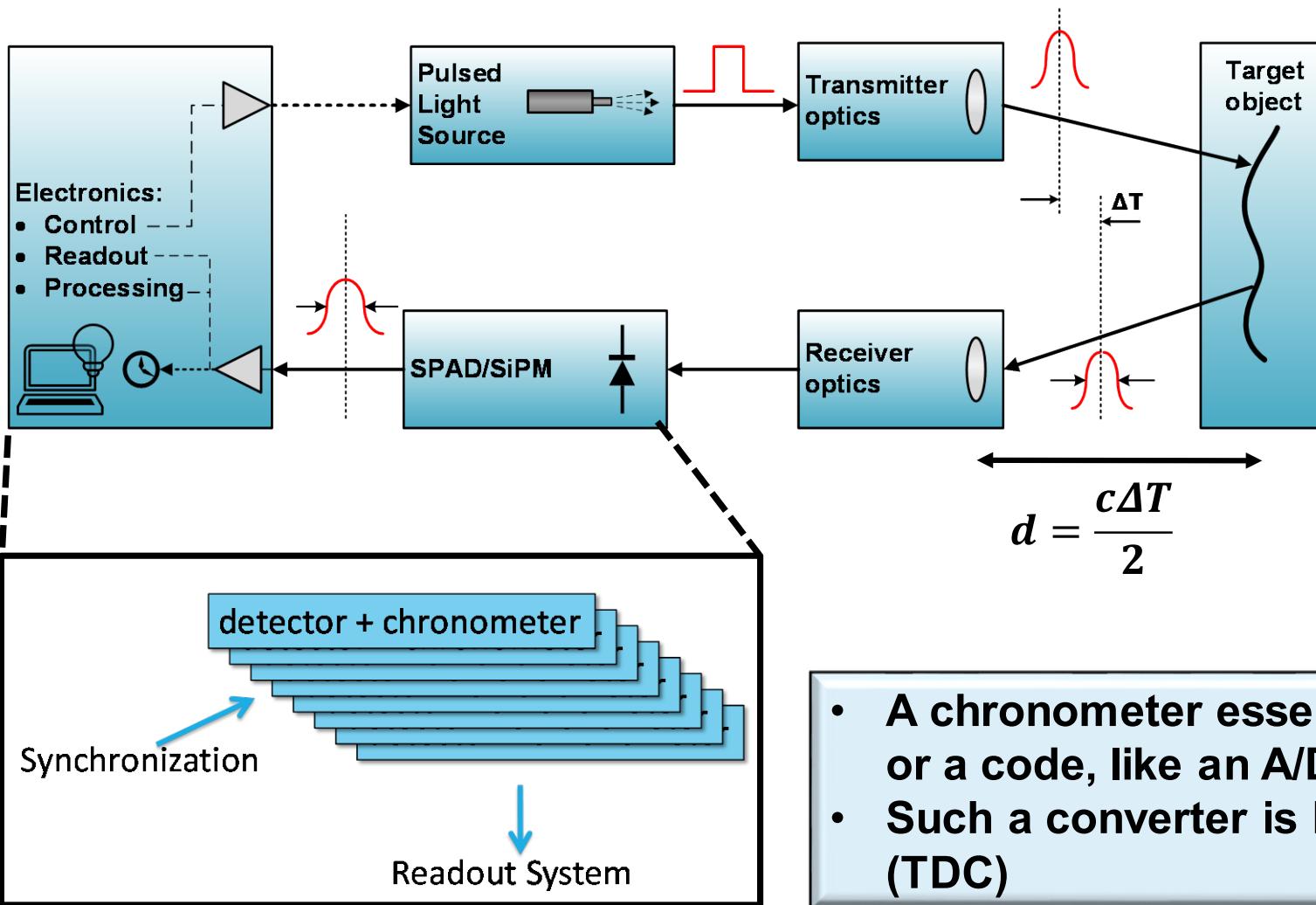
- Assume that a given process triggered by light produces photons with a certain probability distribution function  $PDF(t)$
- Then one can measure it by repeating a measurement of a single photon time-of-arrival  $N$  times and building a frequency statistics known as histogram  $h(t)$
- It can be shown that:

$$h(t) \rightarrow PDF(t) \text{ for } N \rightarrow \infty$$



- This technique is known as time-correlated single-photon counting (TCSPC)

## 11.3.9 TDC Application Example: Time-of-Flight System



- A chronometer essentially converts time onto a number or a code, like an A/D converter
- Such a converter is known as time-to-digital converter (TDC)

## 11.4 Homework slides (see Exercises)

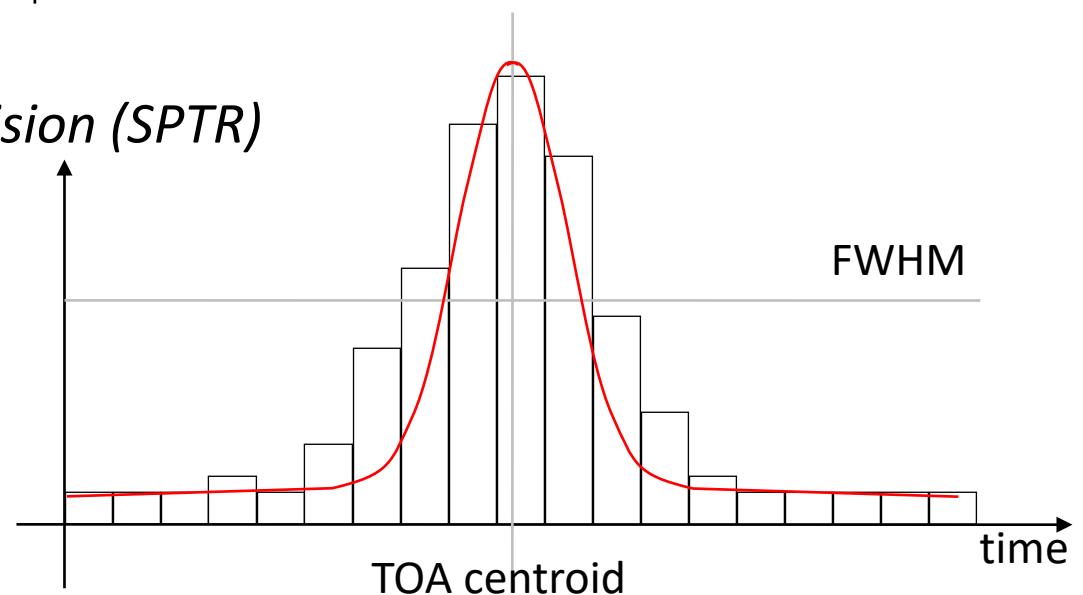
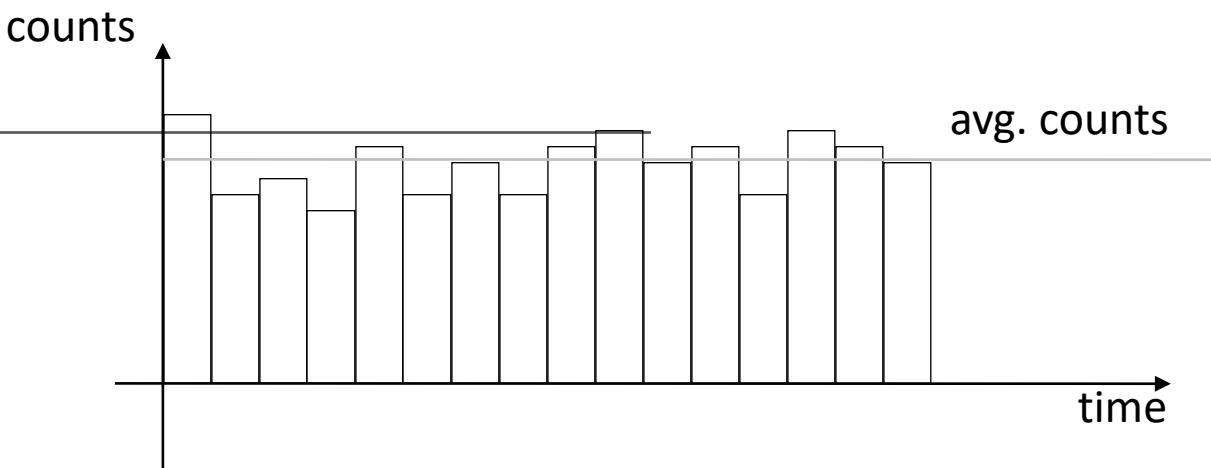
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- Homework 1: Design and analysis of a FLIM System
- Homework 2: Design and analysis of a LIDAR system
- Homework 3: Design and analysis of a PET System

→ These *Case Studies*, based on material from W8-W11, represent possible exam topics.

# Take-home Messages/W11-3

- *Time-to-Digital converters:*
  - *Basics*
  - *INL, DNL*
  - *Metrology: code-density test, single-shot precision (S PTR)*
  - *TDC architectures*
    - *Counter-register*
    - *Delay chain*
    - *Vernier lines*
    - *Ring oscillator*
  - ***Application examples!***



# Acknowledgments

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- Bedirhan Ilik (TA 2019)
- Sergio Cova
- Estelle Labonne
- Akira Matsuzawa